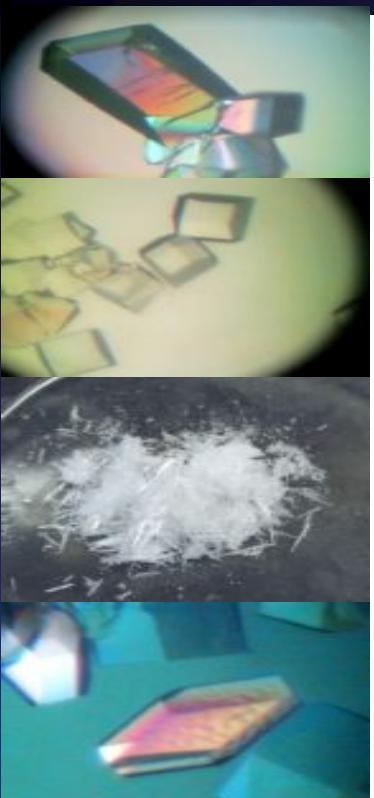


# 결정화 공정의 상평형의 원리와 이해

2007년 8월 20일

결정화 분리기술 사업단

고려대학교 화공생명공학과 강정원

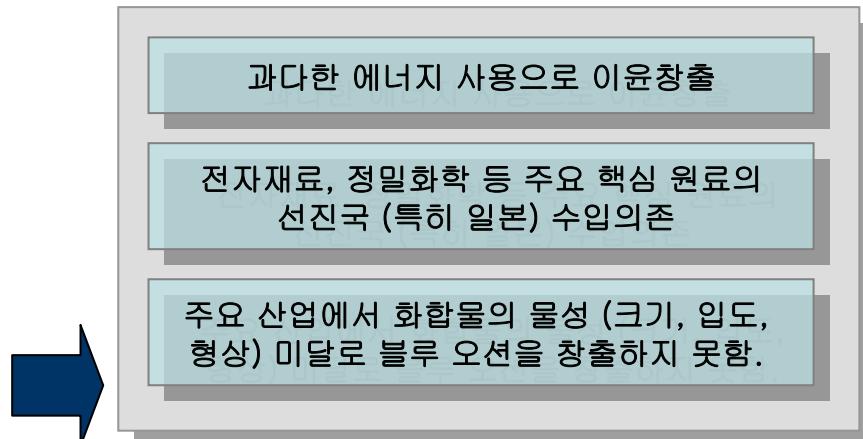


# 1. 서론 - 상평형과 결정화 공정

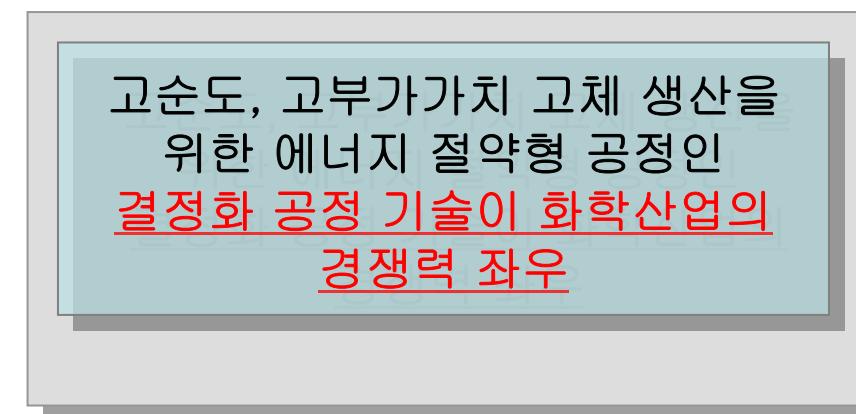
# 21세기 한국 화학공업의 패러다임의 변화



## 현 문제점



## 비전





# Importance of Thermophysical Properties

## ◆ Statistics says ...

- Separation process account for 40-70 % of capital and operating cost in chemical industries
- Physical property errors are costly ...
  - 20 % error in density → 16 % error in equipment size and cost
  - 20 % error in diffusivity → 4 % error in equipment size and cost
  - 10 % error in phase equilibrium
    - Easy-to-separate mixtures : 10 % error in equipment size and cost
    - Hard-to-separate mixtures : 200 % or more error

# Important Thermophysical Properties

## ◆ Important Thermodynamic Properties in Crystallization Processes

- Melting point
- Heat of Fusion
- **Solubility (Phase Equilibrium)**
- Heat of Crystallization
- Heat of Solution
- Heat of Transition
- Supersaturation

Annula total expenditure of BASF on Phase equilibria and themophysical Properties : 8,000,000 Euro p.a. (1993)

Other properties (30 %)

Phase Equilibrium (70 %)

**BASF**



# Basic Considerations ...

## ◆ Crystallization Process

- Involves Solid-Liquid Equilibrium (SLE)
- Solubility information
  - Most basic information required for the design of crystallization processes
  - Sometimes SLE exhibit **complex phase behavior**
    - Examples ) hydrate formation, spinodal decomposition, ....

## ◆ Components involved in SLE

- Solvents
  - Water
  - Nonelectrolytes (Organic compounds)
  - Electrolytes (Inorganic compounds), Ionic Liquids
- Solutes
  - Electrolytes (Inorganic compounds )
  - Nonelectrolytes (Organic Compounds) , ...

# Complex Behavior – Hydrate Formation

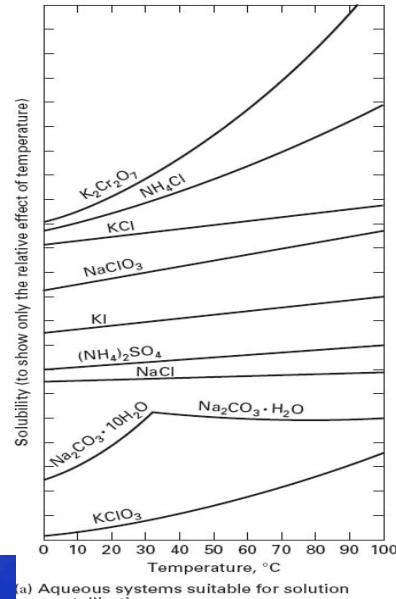
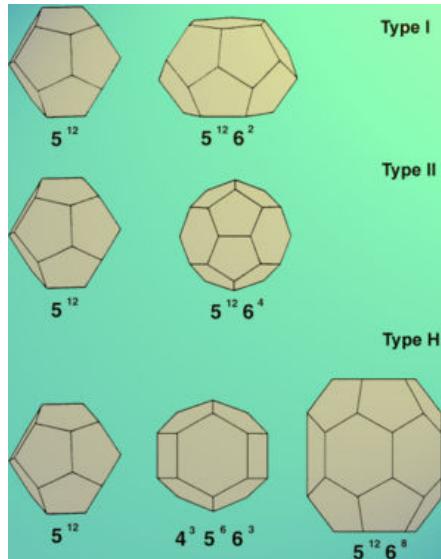
- ◆ **Hydrate** : Solid state containing water
  - Notation : ( hydrous compound ·  $n\text{H}_2\text{O}$  )
  - Example :  $\text{CuSO}_4 \cdot 5\text{H}_2\text{O}$ ,  $\text{Na}_2\text{SO}_4 \cdot 10\text{H}_2\text{O}$ , ...



(chalcanthite)



Gas Hydrate : Clathrate hydrate





# Characteristics of Molecules

## ◆ Intermolecular forces

- Electrostatic forces
  - Coulomb's Law
- Hydrogen bond , Specific (Chemical forces)
  - Not easily explained : Type specific
  - Systems involving –OH, -COOH, ....
- Van der Waals Forces : Nonpolar Intermolecular forces
  - London force
  - Lennard Jones Potential

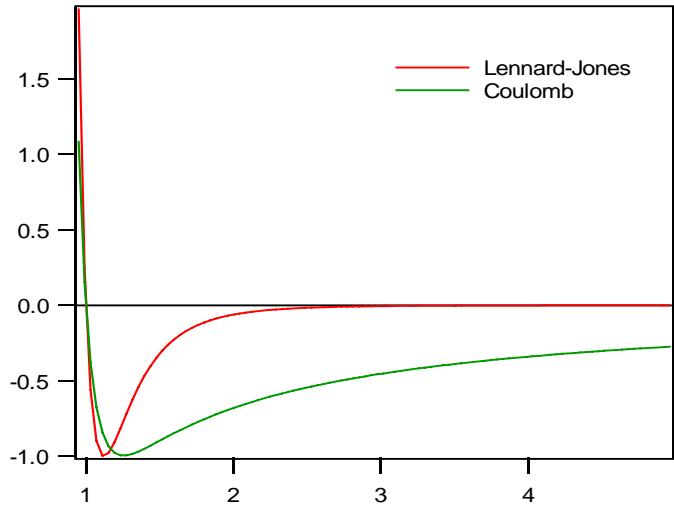
$$\Gamma_{ij} = \frac{q_i q_j}{4\pi\epsilon_0 r}$$

$$\Gamma = 4\epsilon \left[ \left( \frac{\sigma}{r} \right)^{12} - \left( \frac{\sigma}{r} \right)^6 \right]$$



# Intermolecular Forces of Molecules

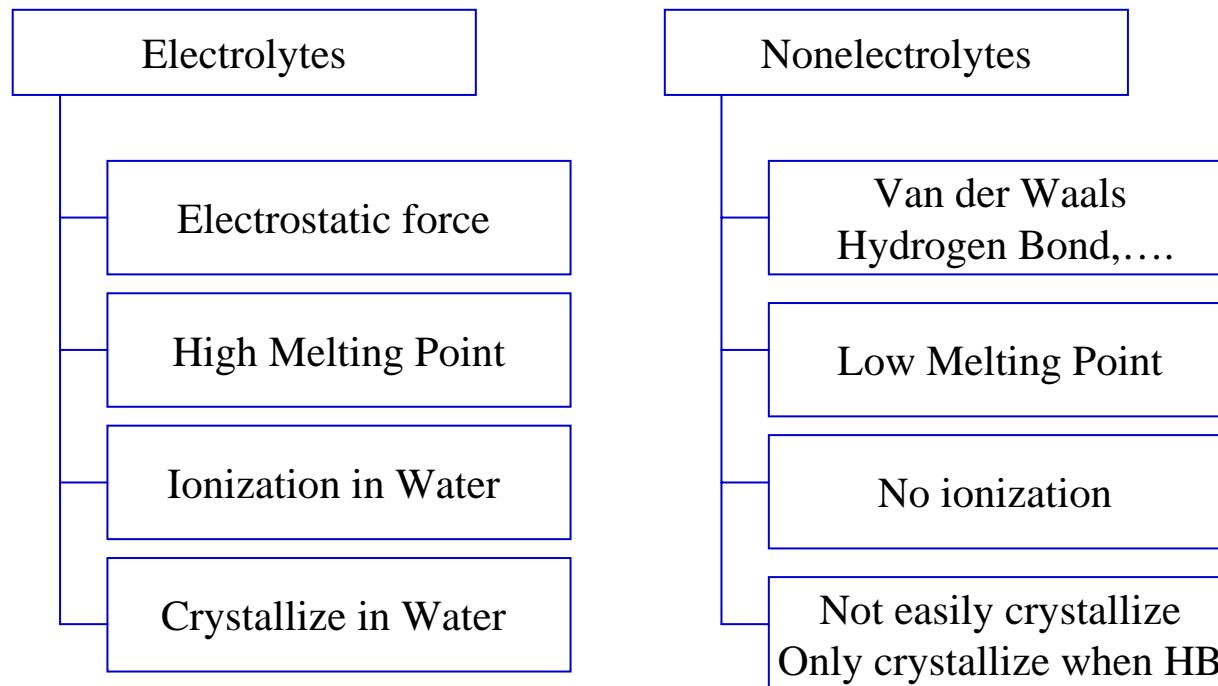
- ◆ Short range forces
  - Dispersion and Repulsion
- ◆ Long range forces
  - Ion-Ion and Dipole-Dipole Interaction



Interaction Type	Dependence	Typical E (kJ/mol)	Comment
Ion-Ion	$1/r$	250	
Ion-Dipole	$1/r^2$	15	
Dipole-Dipole	$1/r^3$	2	Stationary
London	$1/r^6$	2	

# Basic Considerations....

## ◆ Electrolytes vs. Nonelectrolytes



→ Electrolytes are normally appear in Crystalline Structure

→ For nonelectrolyte molecules, specific forces are required to form a crystal



# Crystal vs. Amorphous State

## ◆ Crystal and Amorphous State

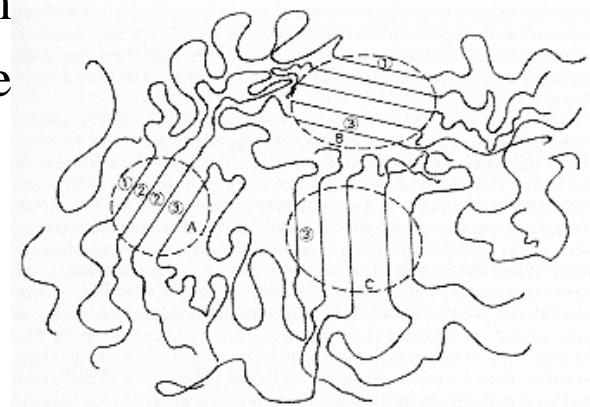
### – Crystal

- Regular arrangement of atoms
- Physical properties depend on the direction of measurement → anisotropic



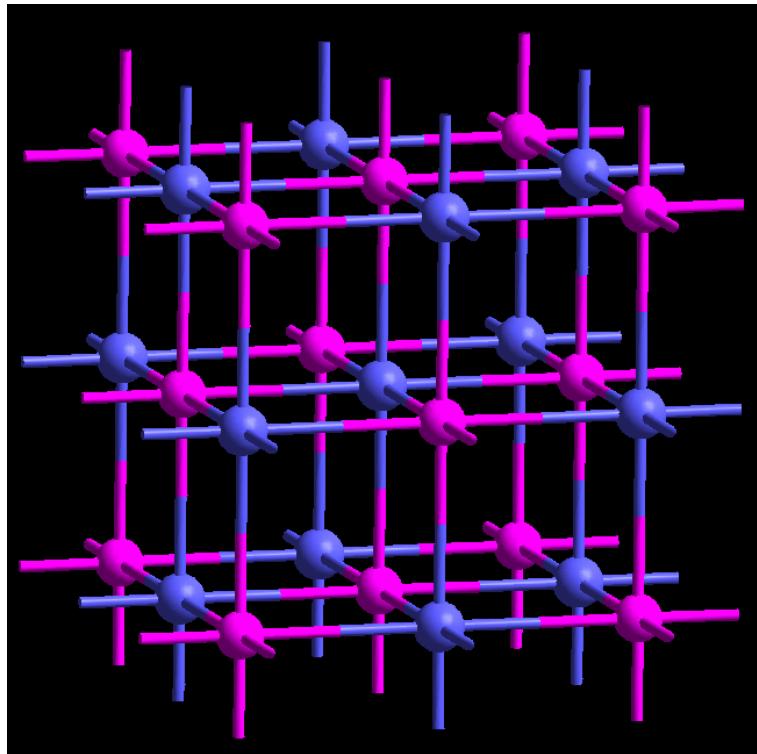
### – Amorphous

- Irregular arrangement of atoms
- Physical Properties are independent of measurements → isotropic

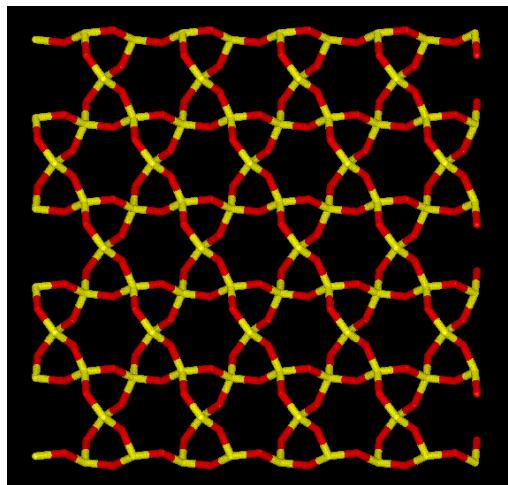




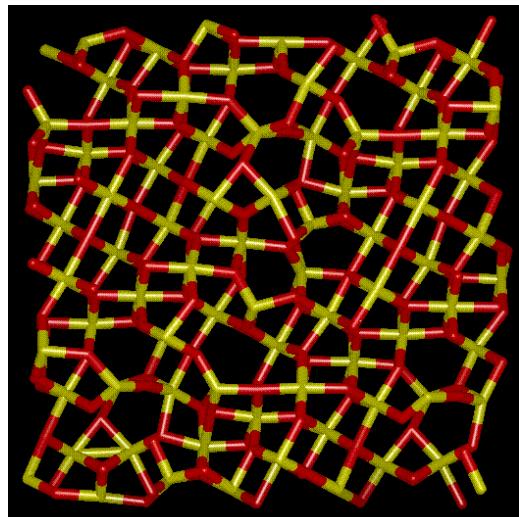
# Crystal vs. Amorphous State...



Crystal Structure of NaCl (Sodium Chloride)  
Fcc lattice structure



SiO<sub>2</sub> : An ordered crystal



SiO<sub>2</sub> : An armophous glass



# Basic Consideration ... Solubility

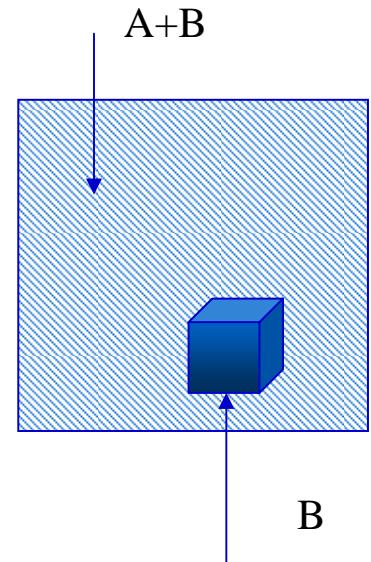
## ◆ Basic Principles to Calculate Solubility

- Solid + Liquid Equilibrium
  - Solids normally exists in pure form
- Equality of **Chemical Potential**

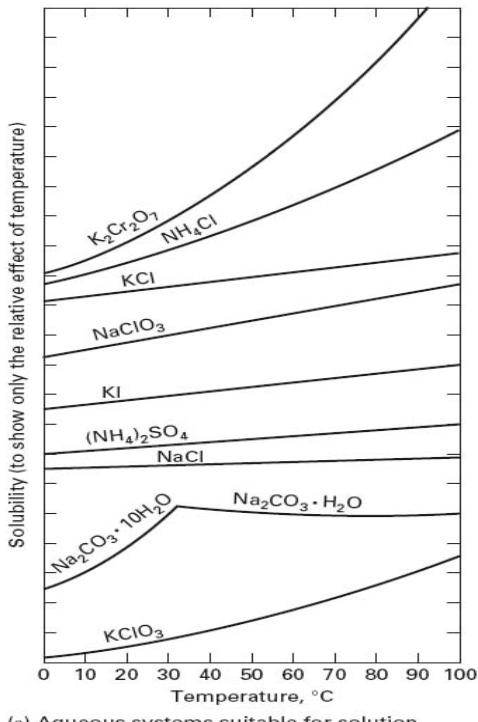
$$\mu_B^{solid}(T, P) = \mu_B^{solution}(T, P, x)$$

- When the meaning of chemical potential is not so clear, **fugacity** can be used instead (units in pressure)

$$f_B^{solid}(T, P) = f_B^{solution}(T, P, x)$$

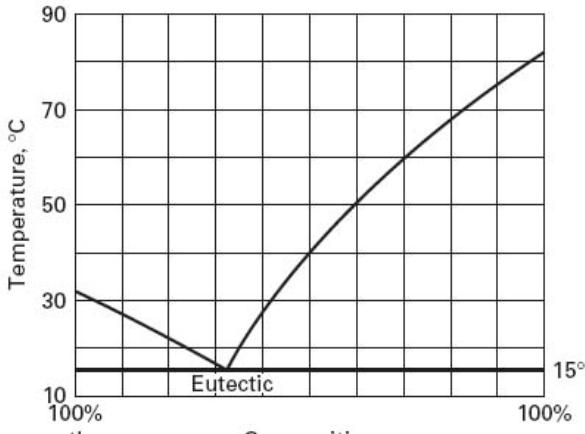


# A Typical SLE Diagrams ...



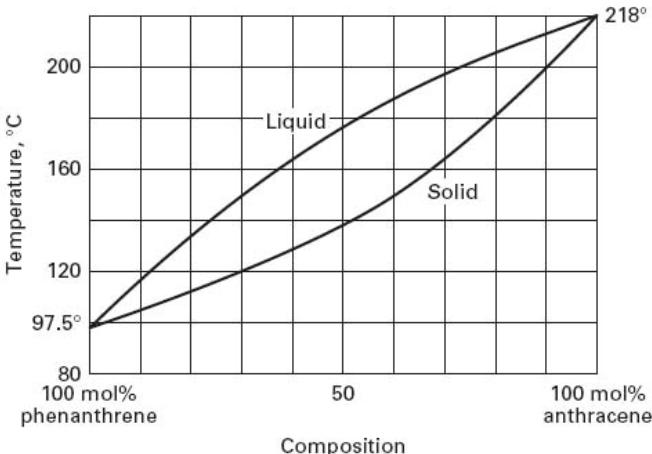
Solution

Far away from melting point of solute  
Near M.P of solute solvent is in gas state

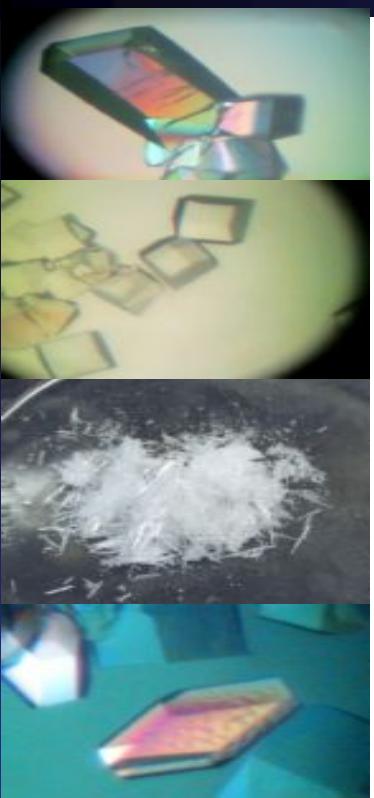


(b) Eutectic-forming system of ortho- and parachloronitrobenzene system suitable for melt crystallization

Melt



(c) Solid-solution system suitable for fractional melt crystallization



## 2. 물성과 용해도 측정



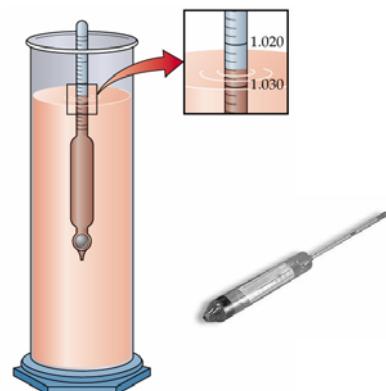
# Density

## ◆ Measurement of density

- Measurements of weight of substances with known volume
  - Pycnometer
  - Hydrometer
  - Insertion Density Transmitters



Pycnometer



Hydrometer



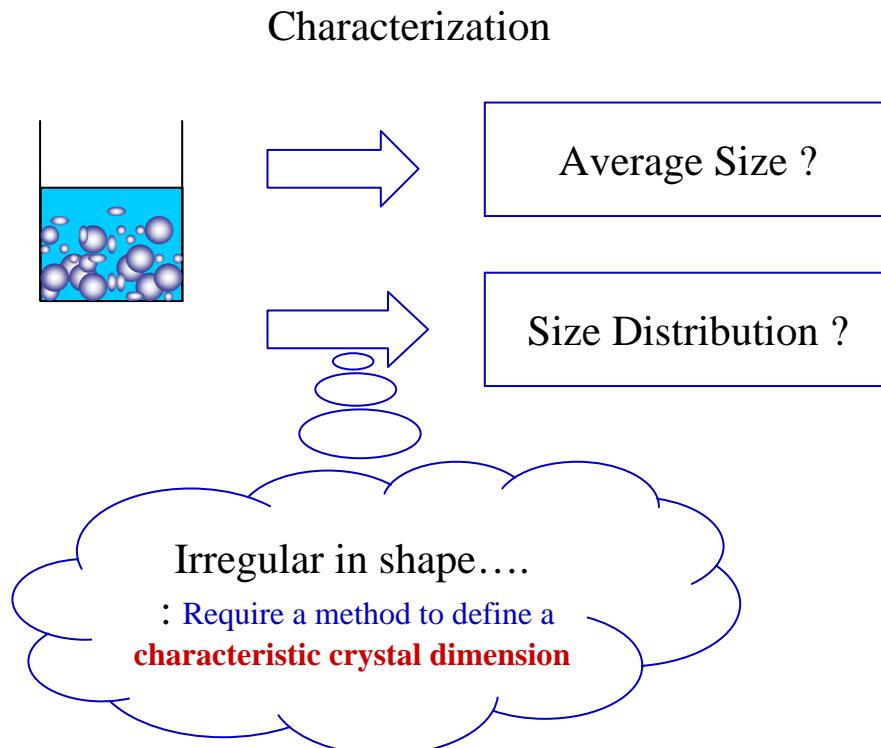
Insertion Density Transmitter



Anton Paar Density Meter  
: Oscillating U-tube method

# Size Classification of Crystals

- ◆ Crystallizers are often operated in batch mode
- ◆ How to characterize a batch of crystals (particles) ?





# Sphericity

$$\psi = \frac{\text{surface area of a sphere with the same volume as particle}}{\text{surface area of the particle}}$$

$\psi = 1$  : sphere

$\psi < 1$  : all other particles

For a sphere particle of diameter  $D_p$

$$\left( \frac{s_p}{v_p} \right)_{sphere} = \frac{\pi D_p^2}{(\pi D_p^3 / 6)} = \frac{6}{D_p}$$

$$\psi = \frac{6}{D_p} \left( \frac{v_p}{s_p} \right)_{particle}$$

# Methods of Measuring Particle Size

Method	Size Range (micron)	Size Range (nm)
Woven-wire screen	32-5600	
Coulter electrical sensor	1-200	
Gravity sedimentation	0.5-1-50	
Optical microscopy	0.5-150	
Laser-light scattering	0.04-2000	40-2000000
Centrifugal sedimentation	0.01-5	10-5000
Electron microscopy	0.001-5	1-5000

Result may differ by **50 %** depending on measurement methods



Standard Sieve



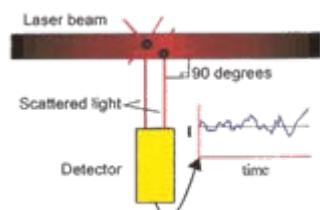
Automatic Sieve Analyzer



Coulter Image Analysis System



Laser-light Scattering



# Particle Size Distribution using Wire-Mesh Screen (Sieve)

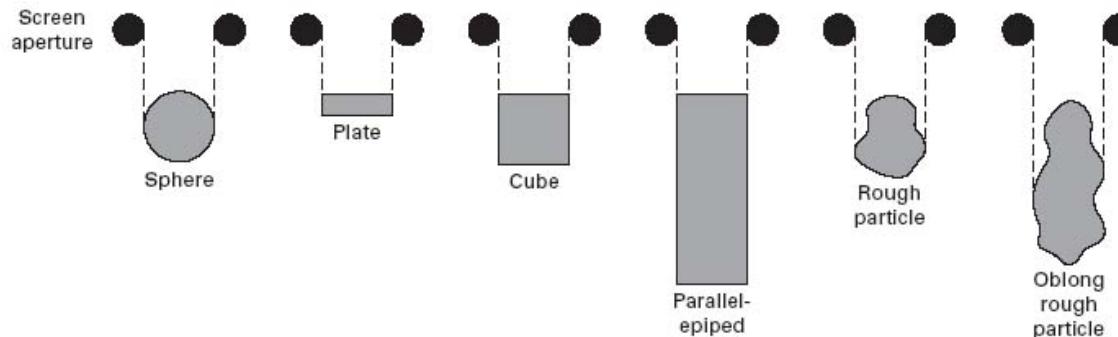
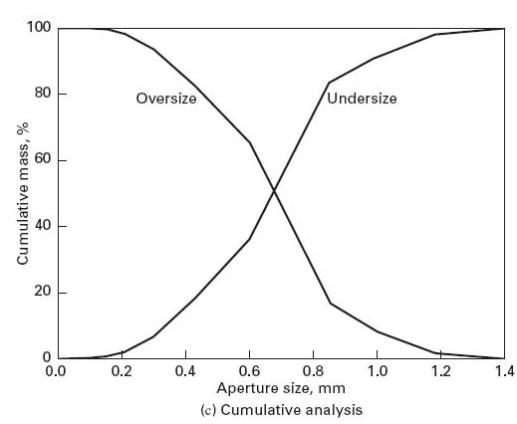
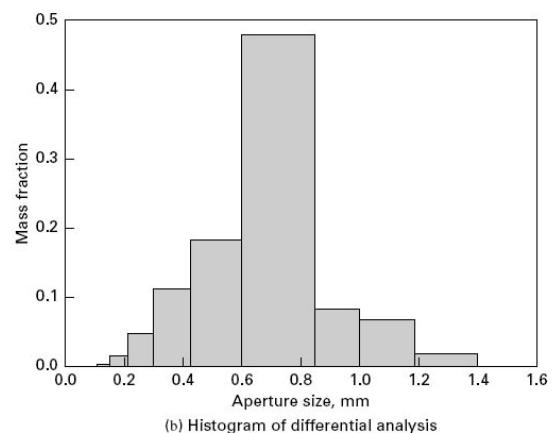
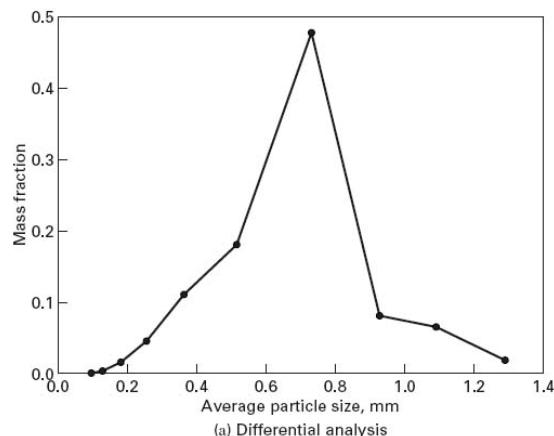


Figure 17.7 Different particle shapes that just pass through the same screen.





# Mean Particle Size

- ◆ Surface-mean diameter
- ◆ Mass-mean diameter
- ◆ Volume-mean diameter



# Measurement of Solubility

## ◆ Elements for Solubility Measurement

- Temperature Control
- Agitation of Solution
- Sampling
- Achievement of Equilibrium

## ◆ Measurement Technique

- Polythermal Method
- Isothermal Method



# Solubility Data Source

- ◆ Dortmund Databank (SLE Database)
- ◆ IUPAC Solubility Data Series