

# Dynamic modeling of activated sludge process

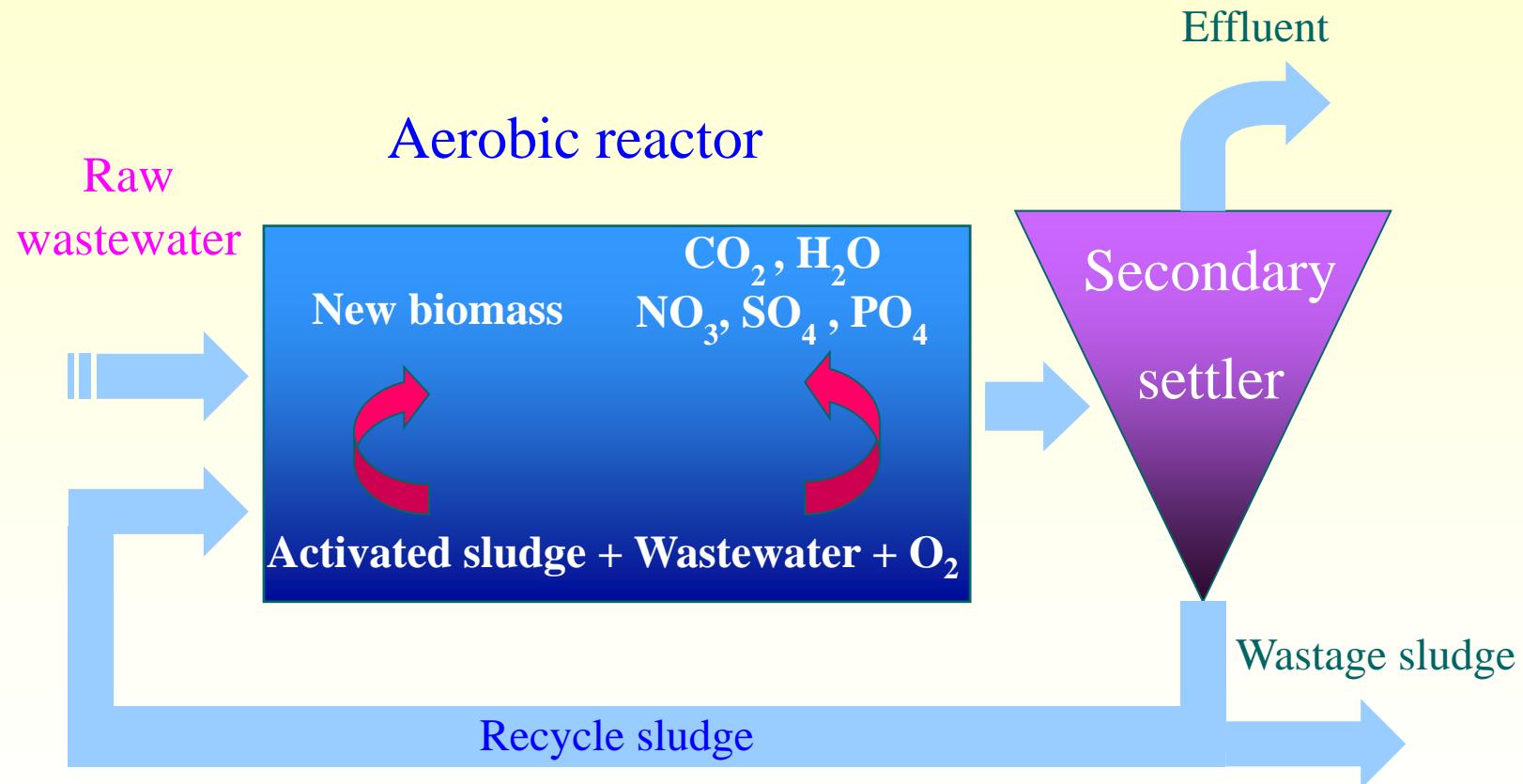
POSTECH  
Department of Chemical Engineering  
PSE Lab.

# 1. Modeling of Activated Sludge Process

- ✓ IAWQ activated sludge model No.1
- ✓ Secondary settler modeling
- ✓ Integrated modeling
- ✓ Benchmark study model (predenitrification process)



## 1.1 Outline of Activated Sludge Process



## 1.2 Modeling

- Bioreactor modeling
  - IAWQ (International Association on Water Quality)  
Activated sludge model No.1 (1987, Henze *et al.*)
- Secondary settler modeling
  - Solid flux theory (1986, Vitasovic)  
and double exponential velocity theory (1991, Takâcs)
- Integrated modeling (predenitrification process)
  - COST682 Working group : Benchmark study model

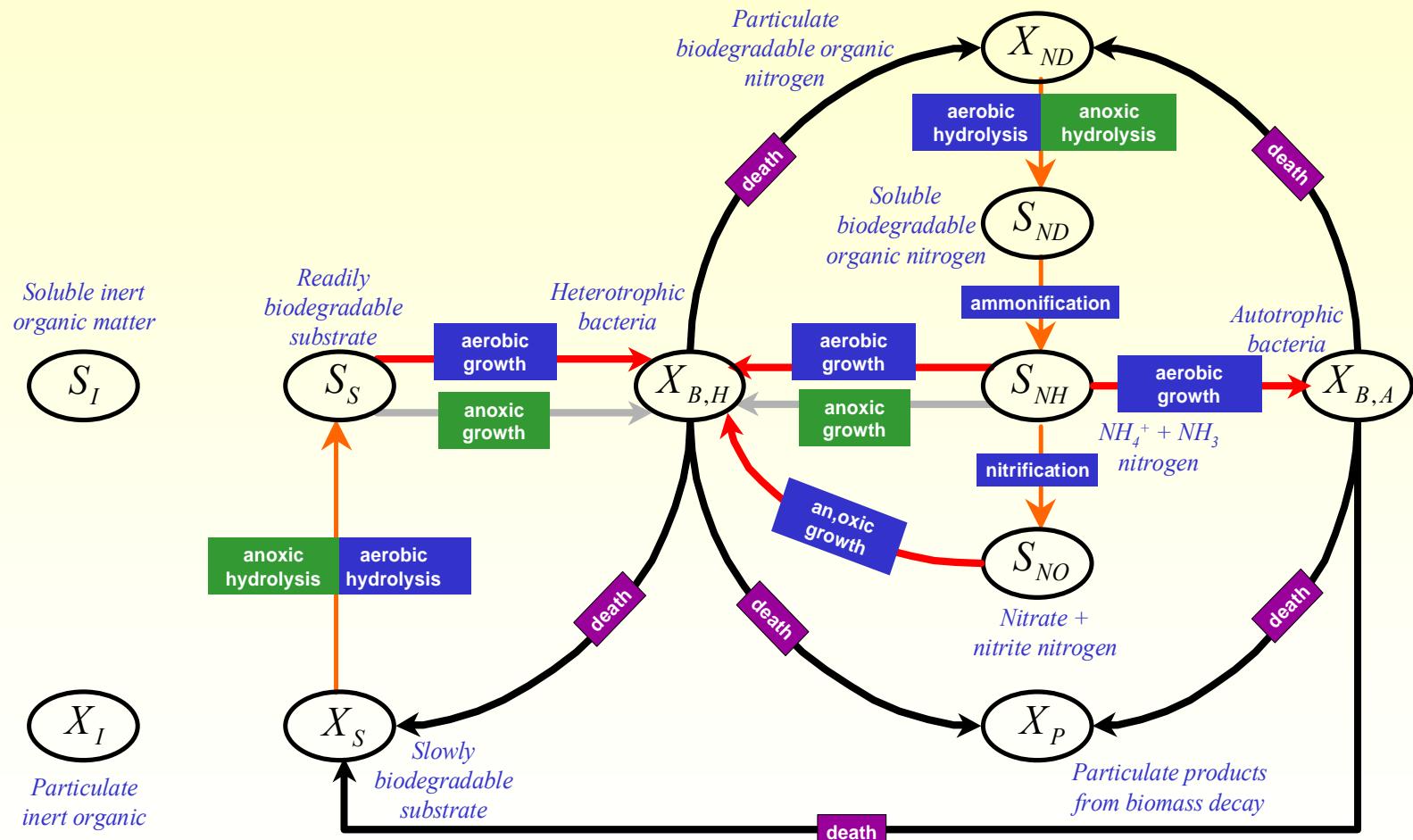


## 1.3 IAWQ ASM No.1 (1)

- 13 components
  - Microorganisms ( $X_{BH}$ ,  $X_{BA}$ )
  - Carbonaceous compounds ( $S_I$ ,  $S_S$ ,  $X_I$ ,  $X_S$ ,  $X_P$ )
  - Nitrogenous compounds ( $S_{NO}$ ,  $S_{NH}$ ,  $S_{ND}$ ,  $X_{ND}$ )
  - Auxiliary states ( $S_O$ ,  $S_{ALK}$ )
- 8 reactions
  - Oxidation of organic carbon, Nitrification, Denitrification, etc.
- Basic structure (mass balance) 
$$\frac{dC_i}{dt} = \frac{Q_{in} C_{i,in} - Q_{out} C_i}{V} + r_i$$



## 1.4 IAWQ ASM No.1 (2)



# 1.5 IAWQ ASM No.1 (3)

## ■ Important equations

$$\frac{dX_{B,H}}{dt} = \left[ \hat{\mu}_H \left( \frac{S_S}{K_S + S_S} \right) \left\{ \left( \frac{S_O}{K_{O,H} + S_O} \right) + \eta_g \left( \frac{K_{O,H}}{K_{O,H} + S_O} \right) \left( \frac{S_{NO}}{K_{NO} + S_{NO}} \right) \right\} - b_H \right] X_{B,H} + \frac{Q_{in}}{V} X_{B,H,in} + \frac{Q_r}{V} X_{B,H,r} - \frac{Q}{V} X_{B,H}$$

$$\begin{aligned} \frac{dS_S}{dt} = & \left[ -\frac{\hat{\mu}_H}{Y_H} \left( \frac{S_S}{K_S + S_S} \right) \left\{ \left( \frac{S_O}{K_{O,H} + S_O} \right) + \eta_g \left( \frac{K_{O,H}}{K_{O,H} + S_O} \right) \left( \frac{S_{NO}}{K_{NO} + S_{NO}} \right) \right\} \right. \\ & \left. + k_h \frac{X_S/X_{B,H}}{K_X + (X_S/X_{B,H})} \left\{ \left( \frac{S_O}{K_{O,H} + S_O} \right) + \eta_h \left( \frac{K_{O,H}}{K_{O,H} + S_O} \right) \left( \frac{S_{NO}}{K_{NO} + S_{NO}} \right) \right\} \right] X_{B,H} \\ & + \frac{Q_{in}}{V} S_{S,in} + \frac{Q_r}{V} S_{S,r} - \frac{Q}{V} S_S \end{aligned}$$

$$\frac{dS_O}{dt} = -\hat{\mu}_H \left( \frac{1-Y_H}{Y_H} \right) \left( \frac{S_S}{K_S + S_S} \right) \left( \frac{S_O}{K_{O,H} + S_O} \right) X_{B,H} - \hat{\mu}_A \left( \frac{4.57-Y_A}{Y_A} \right) \left( \frac{S_{NH}}{K_{NH} + S_{NH}} \right) \left( \frac{S_O}{K_{O,A} + S_O} \right) X_{B,A} + K_L a (S_{O,sat} - S_O)$$



# 1.6 Modeling of Secondary Settler

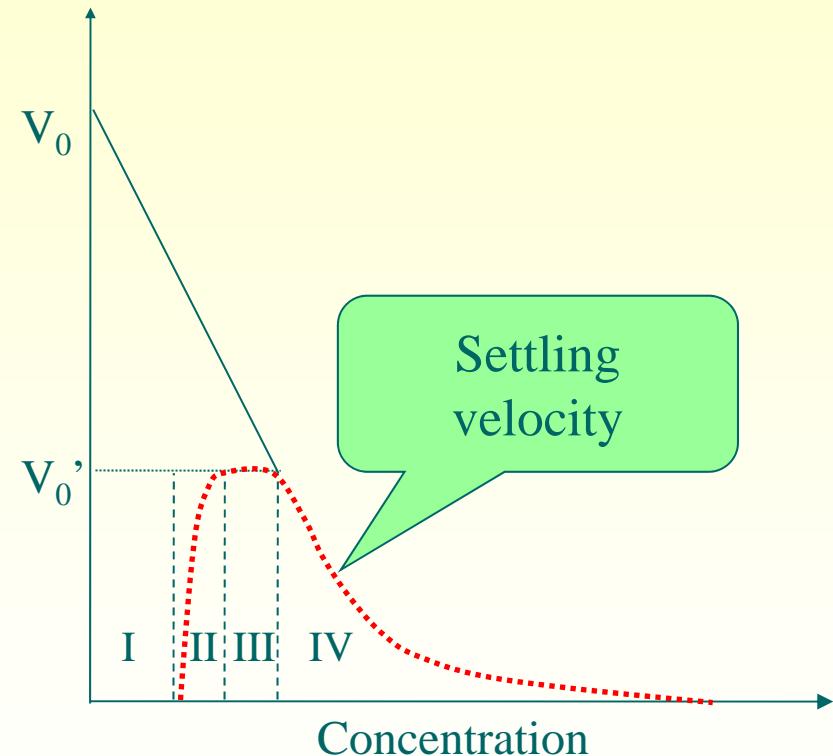
- Solid flux theory

$$J = J_s + J_{dn}, \quad J_j = X_j v_{sj} + X_j v_u$$

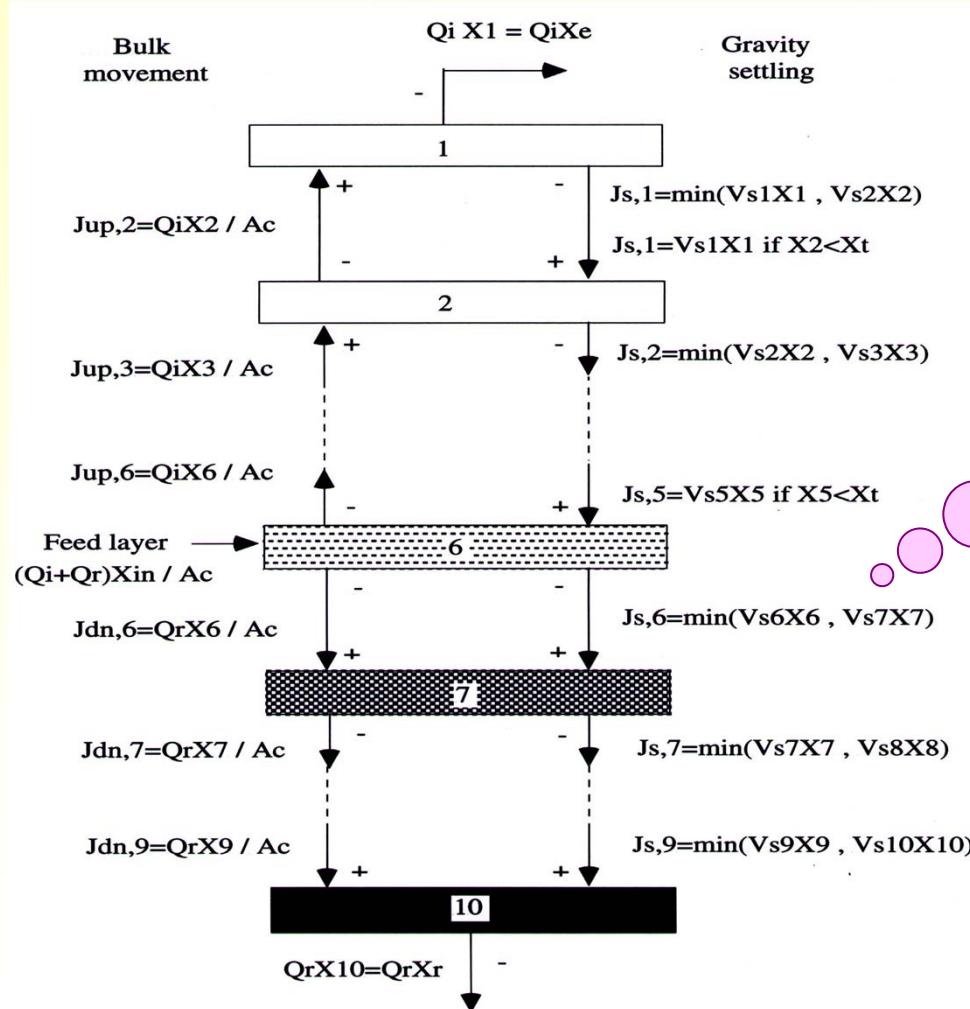
(bulk movement + gravity settling)

- Double exponential-velocity theory

$$v_{sj} = v_0 e^{-r_h X_j^*} - v_0 e^{-r_p X_j^*} \quad (0 \leq v_{sj} \leq v_0)$$



# 1.7 General Settler Model



Limiting solid flux



## 1.8 Integrated Modeling

- Combination of reactor and settler

$$\frac{X_{S,5}}{X_f} = \frac{X_{S,u}}{X_u} \quad (\text{fraction equality})$$

- Predenitrification process

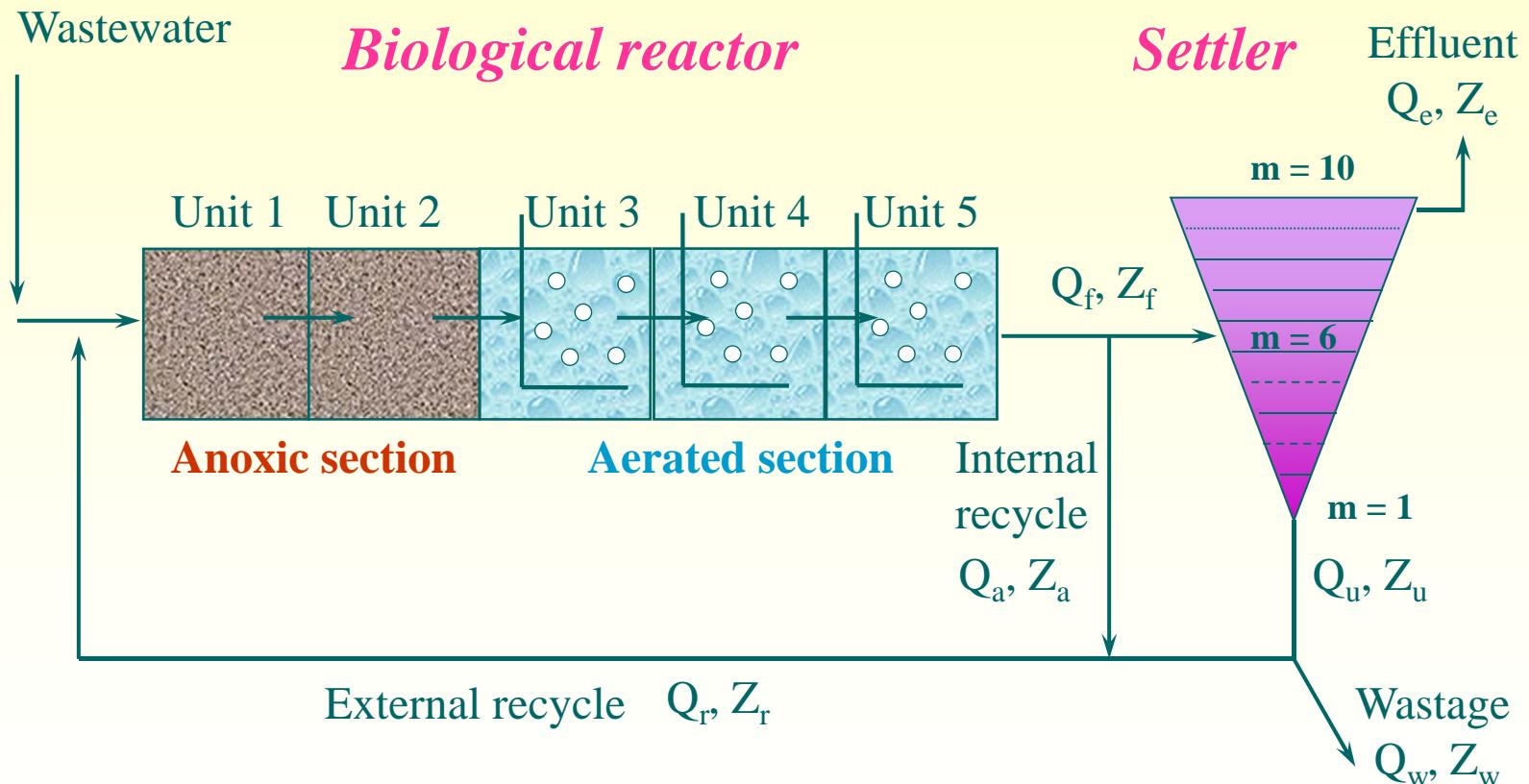
- Advanced wastewater treatment process (nitrogen removal)
- The most economic nitrogen removal process (1991, Henze)
- Benchmark study model (COST 682 & 624 Group)



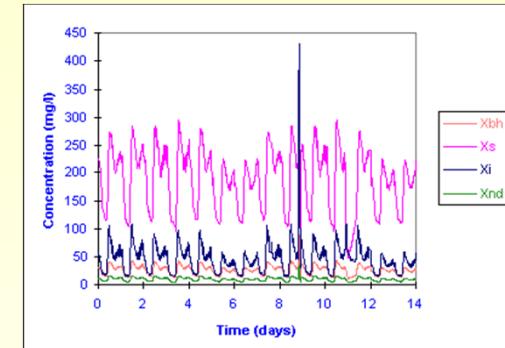
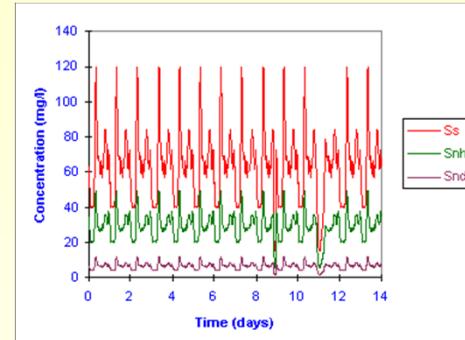
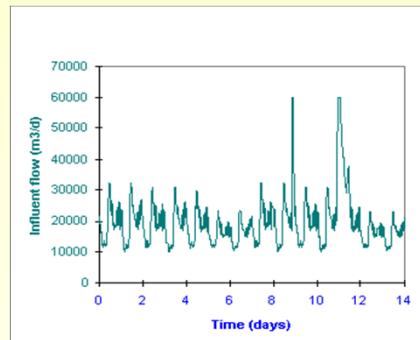
- Five-compartment reactor and secondary settler



# 1.9 Benchmark Study Model



# 1.10 Simulation Results



Storm-weather  
condition

