

Chapter 4. Liquid-Gas and Liquid-Liquid Interface

surface 분자들은 안쪽으로 힘을 받는다.

- surface tension : 모든 물질이 구형이 되려는 성질

단위면적당 surface free energy $G^s = \gamma A$

surface 에 위치한 분자

⇒ force unbalance에 의하여 힘을 inward 방향으로 받음.

단위면적을 generation하는데 필요한 $E = \gamma$

γ (surface science ; surface에서 단위면적당 Gibbs free energy) $\Leftrightarrow G$ (in bulk material)

γ 의 단위 : energy per unit area (erg/cm²)

$$\text{erg/cm}^2 = 1 \text{ dyn} \cdot \text{cm/cm}^2 = \text{dyn/cm} = \text{단위길이당 힘}$$

- Turbulence in molecular level at surface

at equilibrium 증발속도=응축속도

1.2×10^{22} molecules/cm² · sec at 25°C for H₂O

For H₂O 72.8 dyn/cm = 72.8 erg/cm²

For Hg 485 dyn/cm = 485 erg/cm²

surface energy(tension)이 매우 커서 drop → 모양 변화없음

- Surface science에서 알아야 할 것

- Laplace-Young Eq.
- Kelvin Eq.
- Gibbs Adsorption Eq.

① Laplace-Young Eq

$$\text{work} = (\Delta P)(\Delta V) = (\Delta P)(4\pi r^2 dr)$$

T, P등이 일정유지되면,

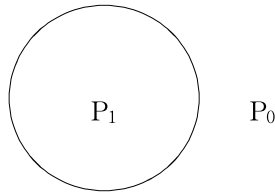
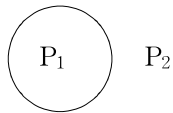
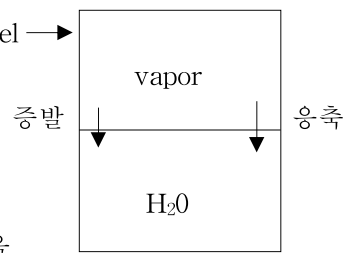
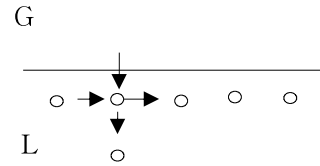
$$\text{energy 변화량} = 4\pi(r+dr)^2 \cdot \gamma[\text{나중상태}] - 4\pi r^2(r+dr)^2 \cdot \gamma[\text{초기상태}]$$

$$= 4\pi\gamma((r+dr)^2 - r^2)$$

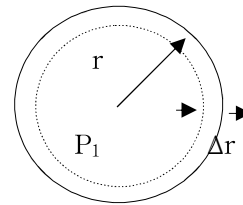
$$= 4\pi\gamma(r^2 + 2rdr + (dr)^2 - r^2)$$

$$= 4\pi\gamma \cdot 2rdr = 8\pi\gamma r dr = \Delta P 4\pi r^2 dr$$

$$\therefore \Delta P = 2\gamma/r \quad r \text{이 작을수록 } \Delta P \uparrow \quad P_2$$



$$P_2 > P_1 > P_0$$



surface (viscosity) : g/cm

N/m

bulk (") : g/cm-sec

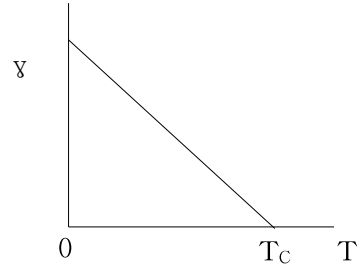
N/m²

$$\gamma \left[\frac{Mx}{P} \right]^{2/3} = k(T_c - T - b)$$

- Variation of γ with pressure in bulk $dG = Vdp - SdT$
at surface $dG^s = V^s dp - S^s dT = d\gamma$

$$\left(\frac{d\gamma}{dp} \right)_T = V^s(+)$$

$\therefore \gamma \uparrow$ as $P \downarrow$



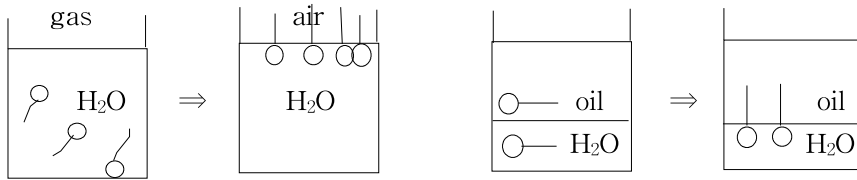
- surfactants(계면활성제) : surface active agent

계면(or 표면)에 흡착해서 계면(or 표면) 물성을 크게 변화시켜주는 물질
분자구조 \Rightarrow 한분자내에 친수성부분과 친유성부분이 동시에 존재하는 물질



친수성 친유성

ex) 지방산 + Glucose(설탕) \longrightarrow 지방산-Glucose



unstable

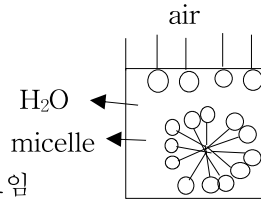
- surfactant의 특징

① 표면물성 변화

② 용액내에서 aggregate 형성

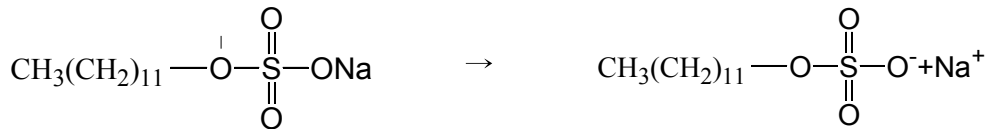
self-assembly oily if 벤젠등을 넣으면 이 부분에서 녹는다
크기: $\sim 100 \text{ \AA}$ (투명하게 보임) 가시광선의 1/4이하면 투명하게 보임

...물과 기름 섞어서 계면활성제에 쓰면 투명하게 보일수 있다.



- surfactant의 분류 : 수용액내에서 이온화되었을 때 surface active part의 ion종류에 따라 분류

① 음이온성: 수용액에 이온화되었을 때 surface active part가 음이온성

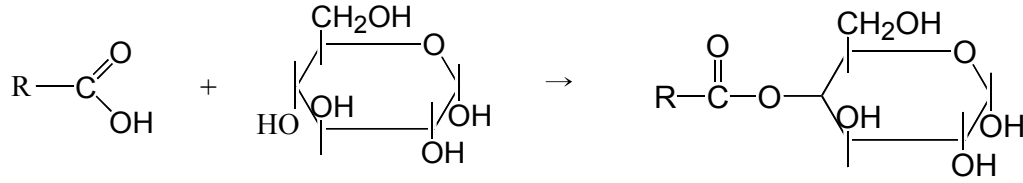


② 양이온성: 수용액에 이온화되었을 때 surface active part가 양이온성

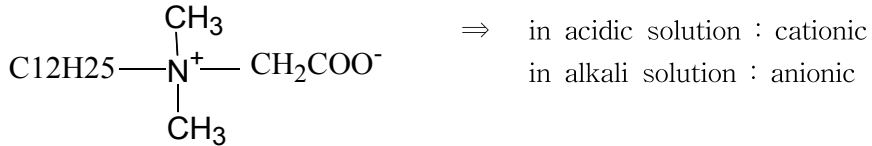


\Rightarrow 헤어린스, 금속표면부식방지제

③비이온성:한분자내에 친수성과 친유성이 존재하나 수용액내에서 이온화되지 않는 surf.

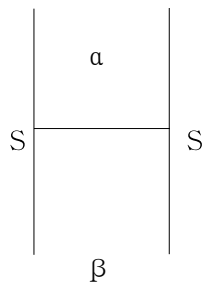
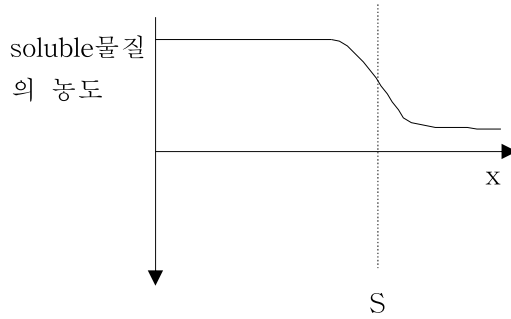
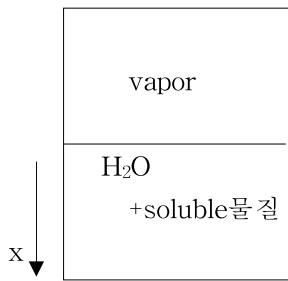


④양쪽성:수용액의 pH에 따라 이온성이 변화되는 것

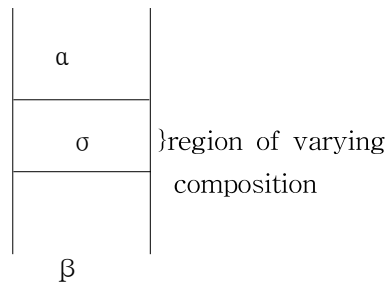


• Thermodynamics of adsorption

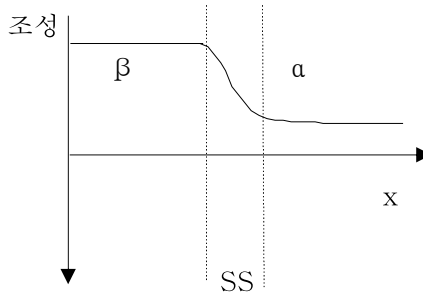
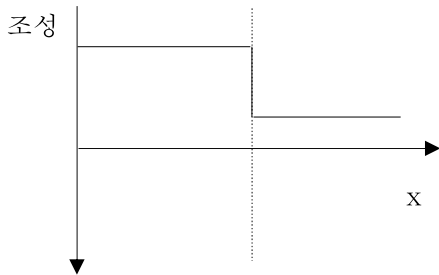
⇒ Gibbs adsorption equation for soluble material인 경우



ideal case



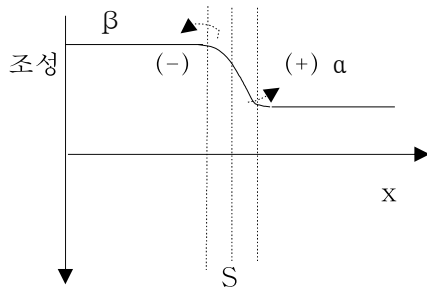
real case



interface를 맘대로 정할수 있다
 ⇒물리적 조성등이 이후에 각각 정한거에 따라 결정됨

• surface excess concentration

n_i^σ : amount of component i in the interfacial phase σ in excess of that which would have been in σ had the bulk phase α and β extended to a surface ss with unchanging composition



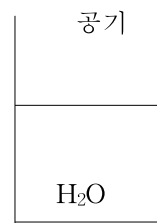
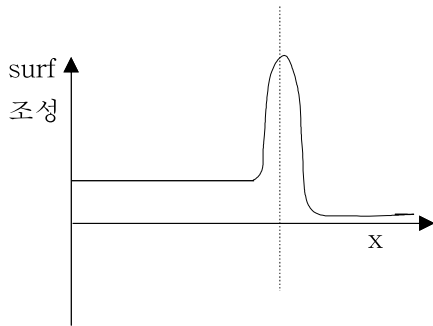
$$n_i^\sigma = A - B$$

surface excess concentration

$$\Gamma_i^\sigma = n_i^\sigma / (\text{interfacial area})$$

: σ phase (interfacial phase)에 존재하는 i 성분의 양을 interfacial area로 나눈 값

for surface active agent



$\Gamma_i^\sigma =$ positive

0 for a given system depending upon the position of ss
negative

• Internal Energy \Rightarrow for open bulk system

$$U = TS - PV + \sum \mu_i n_i$$

\Rightarrow for open interfacial phase

$$U = TS - PV + \gamma A + \sum \mu_i n_i$$

$$U^\sigma = TS^\sigma - PV^\sigma + \gamma A + \sum \mu_i n_i^\sigma$$

at equilibrium $T^\alpha = T^\beta = T^\sigma = T$

$$P^\alpha = P^\beta = P^\sigma = P$$

$$\mu_i^\alpha = \mu_i^\beta = \mu_i^\sigma = \mu_i$$

미분하면 $du^\sigma = T ds^\sigma + S^\sigma dT - P dv^\sigma - V^\sigma dp + \gamma dA + A d\gamma + \sum \mu_i n_i^\sigma + \sum n_i d\mu_i$ ①

From the first law of thermodynamics (에너지 보존 법칙)

$$\Rightarrow du^\sigma = T ds^\sigma - P dv^\sigma + \gamma dA + \sum \mu_i n_i^\sigma$$
 ②

$$\text{cf) } du = T ds - P dv + \sum \mu_i dn_i + \gamma dA$$

from eqn. ① & ②

$$\text{①} - \text{②} \quad S^\sigma dT - V^\sigma dp + A d\gamma + \sum n_i^\sigma d\mu_i = 0$$

at constant T, P ($dT = dp = 0$)

$$A d\gamma + \sum n_i^\sigma d\mu_i = 0$$

$$\therefore d\gamma = \sum_i \frac{\mu_i^\sigma}{A} d\mu_i = - \sum \Gamma_i d\mu_i$$

for binary system

$$d\gamma = -\Gamma_A d\mu_A - \Gamma_B d\mu_B$$

if, $\Gamma_A=0$ 이 되도록 driving surface를 선택하면

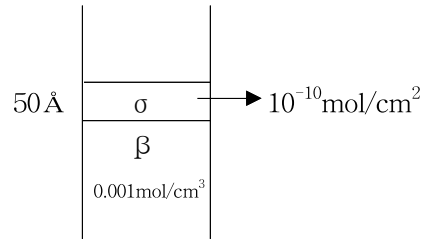
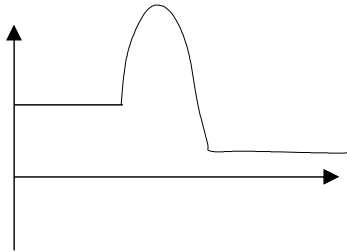
$$d\gamma = -\Gamma_B d\mu_B$$

그런데, $\mu_B = \mu_B^s + RT \ln a_B$ s: standard

$$d\mu_B = RT \ln a_B$$

$$d\gamma = -\Gamma_B RT \ln a_B \rightarrow -\Gamma_B RT \ln C_B \quad \therefore \Gamma_B = -\frac{1}{RT} \frac{d\gamma}{d \ln C_B}$$

$\Gamma_B = 10^{-10} \text{ mol/cm}^2$ at surface \Rightarrow 이걸 2차원으로 바꾸면 C_B 보다 1000배는 큼
 $C_B = 0.001 \text{ mole/cm}^3$ in bulk



for diluted binary system (i.e. non-ionic surfactant)

$\text{H}_2\text{O} \Rightarrow A$ non-ionic surfactant $\Rightarrow B$

$$\Gamma_B = -\frac{1}{RT} \frac{d\gamma}{d \ln C_B}$$

for diluted binary system (i.e. ionic surfactant)

$$d\gamma = \Gamma_i d\mu_i$$

$$= \Gamma_A d\mu_A - \Gamma_B d\mu_B - \Gamma_C d\mu_C = -2\Gamma_B d\mu_B$$

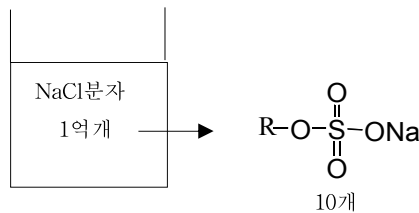
$\Gamma_B = \Gamma_C$ (electroneutrality condition), $\mu_B = \mu_C$

$$\mu_B^s + RT \ln a_B = \mu_C^s + RT \ln C_B$$

$$\mu_C^s + RT \ln a_C = \mu_C^s + RT \ln C_C \quad \therefore \Gamma = -\frac{1}{2RT} \frac{d\gamma}{d \ln C_B}$$

In the presence of excess electrolyte of ionic surfactant

$$\Gamma = -\frac{1}{RT} \frac{d\gamma}{d \ln C_B}$$



counterion이랑 같은 ion이 들어갈 때 $\Gamma_C d\mu_C = 0$

• Surfactant and Interfacial Tension의 측정법

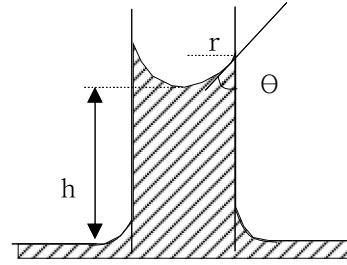
① Capillary rise method

Capillary내 유체에서의 force balance.

중력= surface tension force

$$\pi r^2 h \Delta \rho g = 2 \pi r \gamma \cos \theta \quad \Delta \rho = \rho_L - \rho_G (\text{부력})$$

$$\therefore \gamma = \frac{r \Delta \rho g h}{2 \cos \theta}$$



if, $\theta=0 \Rightarrow$ complete wetting $r = \frac{r \Delta \rho g h}{2}$

for hemi-spherical case

중력= surface tension force

$$\pi r^2 h \Delta \rho g + \left\{ (\pi r^2) \gamma \Delta \rho g - \frac{1}{2} \frac{4}{3} \pi r^3 \Delta \rho g \right\}$$

$$= \pi r^2 h \Delta \rho g + \frac{1}{3} \pi r^3 \Delta \rho g = 2 \pi r \gamma$$

$$\therefore \gamma = \frac{1}{2} r \left(h + \frac{\gamma}{3} \right) \Delta \rho g$$

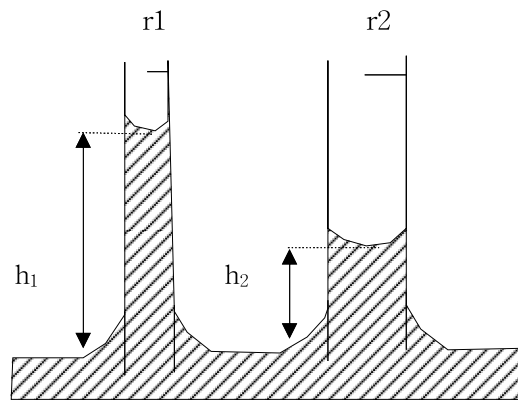
using two capillary tube

$$\gamma = \frac{1}{2} r_1 h_1 \Delta \rho g = \frac{1}{2} r_2 h_2 \Delta \rho g$$

$$h_1 = \frac{\gamma}{\frac{r_1 \Delta \rho g}{2}}, \quad h_2 = \frac{\gamma}{\frac{r_2 \Delta \rho g}{2}}$$

$$\Delta h = h_1 - h_2 = 2 \gamma \frac{1}{\Delta \rho g} \left(\frac{1}{r_1} - \frac{1}{r_2} \right)$$

$$\therefore \gamma = \frac{\Delta \rho g r_1 r_2 \Delta h}{2 (r_2 - r_1)}$$

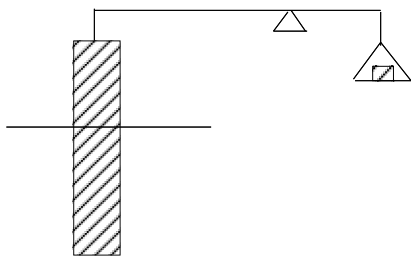


if complete wetting $\Rightarrow \cos \theta$ 무시 ; 재질과 액체가 같으면 $\cos \theta$ 도 같다

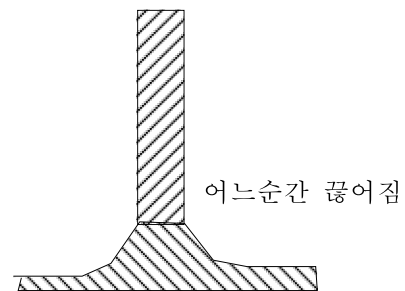
wetting agent \Rightarrow 계면활성제가 들어가면 $\theta=0$ 이 된다. $\Rightarrow \cos \theta=1$ 로 무시

② Wilhelmy Plate method

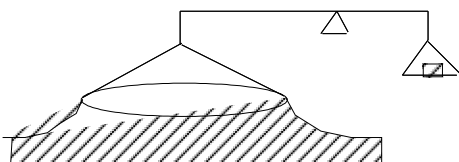
$$W_{\text{total}} = W_{\text{plate}} + 2(x+y)\gamma$$



\Rightarrow
무게를 증가



③ Ring Method



어느순간되면 떨어진다.

$$F = 2(2\pi R)\gamma (\because \text{링의 안쪽과 바깥에서 힘받으므로})$$

④ Drop weight method

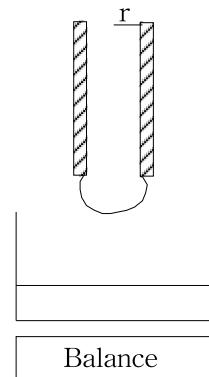
i) non-wetting $mg(\text{drop 1개의 무게}) = 2\pi r\gamma$

$$\gamma = \frac{\Phi mg}{2\pi r} \quad (\Phi: \text{correction factor Fig.4-8})$$

이 경우 error가 많다 \Rightarrow the drop does not leave completely tip
 \Rightarrow surface tension is not exactly vertical

ex) teflon, wax

: 일정방울을 떨어뜨리고 늘어난 무게만큼 divide \Rightarrow 1drop 무게



ii) wetting

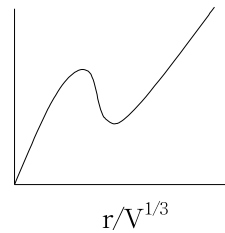
$$mg = 2\pi r' \gamma$$

$$\gamma = \frac{\Phi mg}{2\pi r'}$$

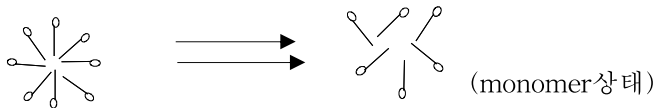
V: drop 1개의 volume

r: tube의 반경

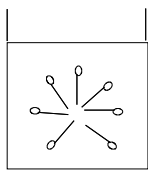
Φ



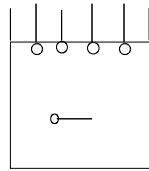
• Association Colloid



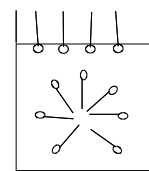
statistical characteristic (통계적)



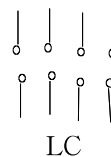
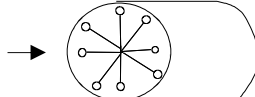
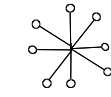
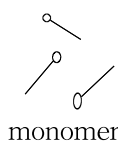
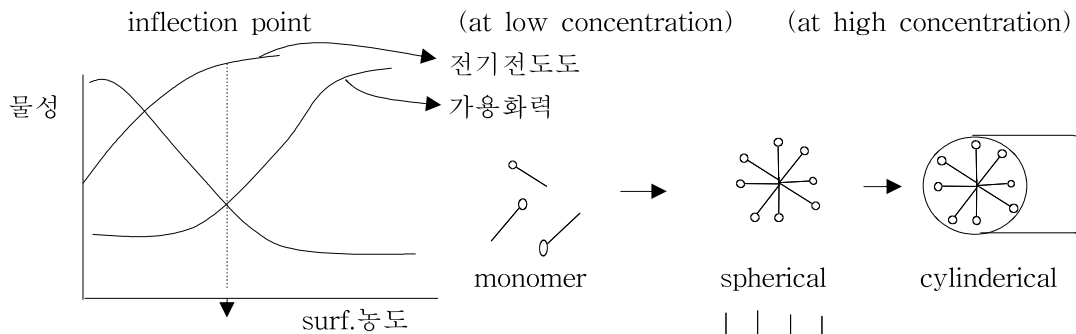
discrete



H₂O



친유성 part는 H₂O로부터 squeeze out



CMC (critical micelle concentration)

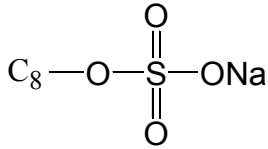
\Rightarrow 눈에 보이지는 않지만 microstructure 됨

cf) Theory Journal of American oil chemists Society

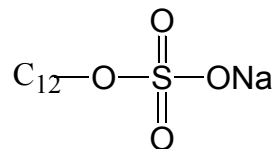
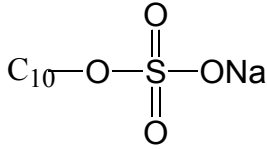
nano tube \Rightarrow H₂ gas 저장

• Factors affecting critical micelle concentration

① CMC ↓ as H.C(hydro carbon)의 길이 ↑ (H.C길이 ↑ 더 낮은 농도에서 spherical 형성)



128mM

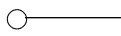


8.0mM

ion성 : 각 탄소길이마다 1/2씩 CMC ↓

non-ion성 : " 1/3 "

② CMC ↑ as T ↑



친수성 친유성 ⇒ micelle의 driving force

③ oraganic molecules

urea(water structure breaker) ⇒ CMC ↑

Fructose, Maltose(water structure promotor) ⇒ CMC ↓

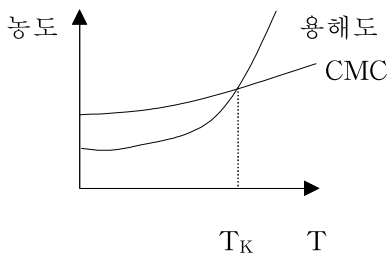
• micelle구조

monomer → spherical → cylindrical → lamellar

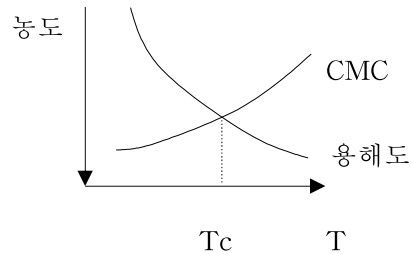
• solublization : water-insoluble 물질이 수용액내에 존재하는 micelle내부로 녹아들어가는 현상

• Krafft point (for only ionic surf)

Clouding point (for only nonionic surf)



: T_K이하에선 micelle 형성안됨



: T_c이상에서 micelle 형성안됨

비이온계면활성제는 T ↑, 용해도 ↓

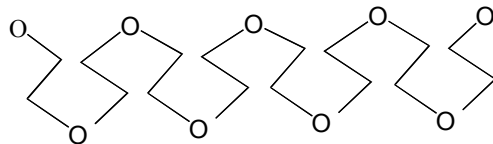
T ↓ chain이 압축되어있어 O가 물과 접촉해서 용해

T ↑ chain이 퍼져서 용해 ↓

-(OCH₂CH₂CH₂)_n 친유성

-(OCH₂CH₂)_n 친수성

-(OCH₂)_n 친유성



• work of adhesion : 다른 종류 column ⇒ $W_{\text{adhesion}} = \gamma_A + \gamma_B - \gamma_{AB}$

work of cohesion : 같은 종류 column ⇒ $W_{\text{adhesion}} = \gamma_A + \gamma_B - \gamma_{AB} \rightarrow 0$

