

## Ch. 7 Charged Surface

• Colloid solid dispersion

①분산의 driving force : 입자간 정전기적 반발력( $V_R$ )

②입자의 aggregation force : 입자간 van der waals force( $V_A$ )

$V_R > V_A \Rightarrow$  stabilize

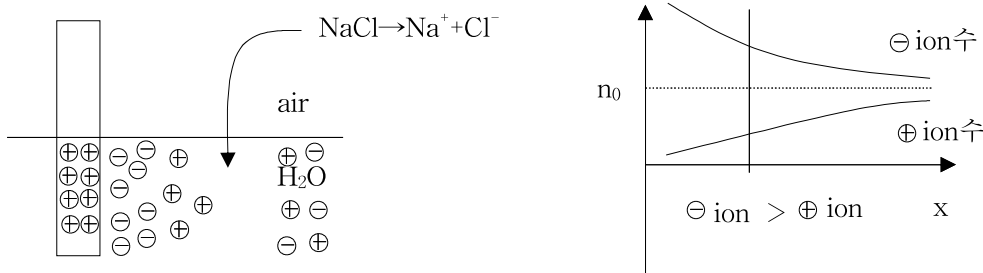
$V_R < V_A \Rightarrow$  aggregation

- H<sub>2</sub>O내에서 solid particle

1)표면의 ion화

2)Ion의 흡착

3)Ion dissolution



by Boltzman Eq.

$$n_+ = n_0 \exp\left(-\frac{ze\psi}{kT}\right)$$

$n_+$ : 단위 부피당 +ion 수

$e$ : electric charge unit(constant)  $E/E_0$

$n_0$ : 단위 부피당 NaCl의 분자수

$\psi$ : electric potential

$z$ : ion의 valency

$$n_- = n_0 \exp\left(+\frac{ze\psi}{kT}\right)$$

net volume charge density

$$\rho = ze(n_+ - n_-) = ze\left\{n_0 \exp\left(-\frac{ze\psi}{kT}\right) - n_0 \exp\left(+\frac{ze\psi}{kT}\right)\right\} = -2zen_0 \sinh\left(\frac{ze\psi}{kT}\right)$$

by Poisson Eq.

$$\frac{d^2\psi}{dx^2} = -\frac{\rho}{\epsilon} \quad \frac{d^2\psi}{dx^2} = \frac{2ze n_0}{\epsilon} \sinh\left(\frac{ze\psi}{kT}\right)$$

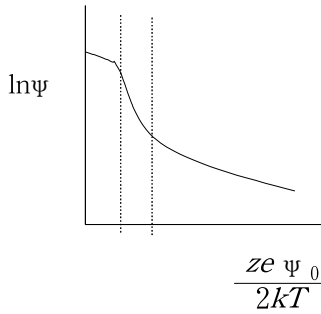
$\epsilon$  : permittivity(constant)

boundary condition

$$\psi = \psi_0 \quad \text{at } x=0$$

$$\psi = 0 \quad \text{or} \quad \frac{d\psi}{dx} = 0 \quad \text{at } x=\infty$$

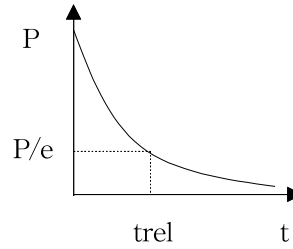
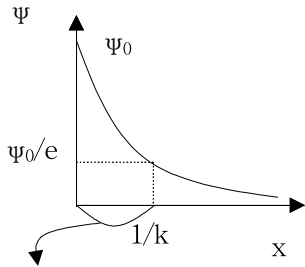
$$\psi = \frac{2kT}{ze} \ln\left[\frac{1 + \gamma \exp(-kT)}{1 - \gamma \exp(-kT)}\right] \quad \gamma = \frac{\exp\left(\frac{ze\psi_0}{2kT}\right) - 1}{\exp\left(\frac{ze\psi_0}{2kT}\right) + 1} \quad k = \left[\frac{2e^2 n_0 z^2}{\epsilon kT}\right]^{\frac{1}{2}}$$



if,  $\frac{ze \psi_0}{2kT} \ll 1.0$

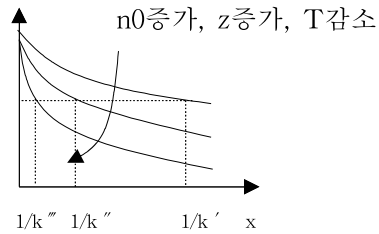
$$\exp\left(\frac{ze \psi_0}{2kT}\right) = 1 + \frac{ze \psi_0}{2kT}$$

$$\therefore \psi = \psi_0 \exp(-kx)$$

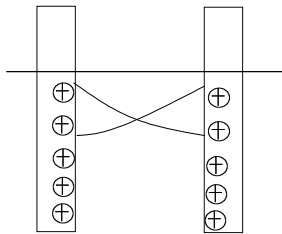


effective double layer thickness (Debye-Hückel length)

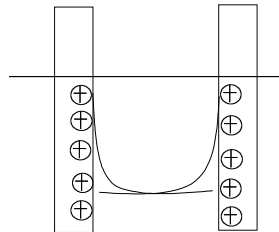
$$k = \left[ \frac{2 e^2 n_0 z^2}{EkT} \right]^{1/2}$$



$$n_0 \uparrow, z \uparrow, T \downarrow \Rightarrow k \uparrow \Rightarrow 1/k \downarrow, \psi/e$$



느리게 가라앉음

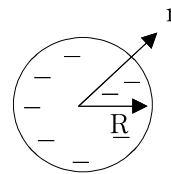


빨리 가라앉음

• Spherical

$$\nabla^2 \psi = -\frac{1}{r^2} \frac{d}{dr} \left( r^2 \frac{d\psi}{dr} \right)$$

$$\frac{d^2 \psi}{dr^2} = -\frac{2ze n_0}{E} \sinh \frac{ze\psi}{kT}$$



B.C.1  $\psi = \psi_0$  at  $r = R$

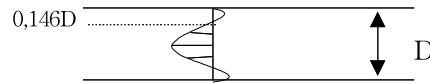
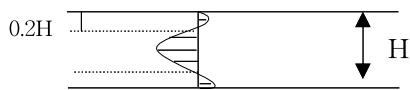
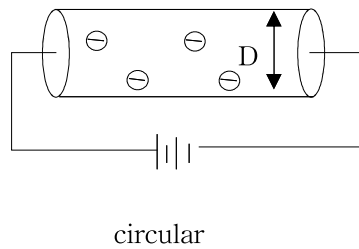
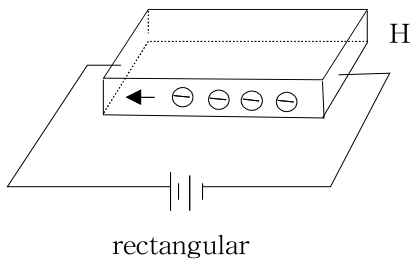
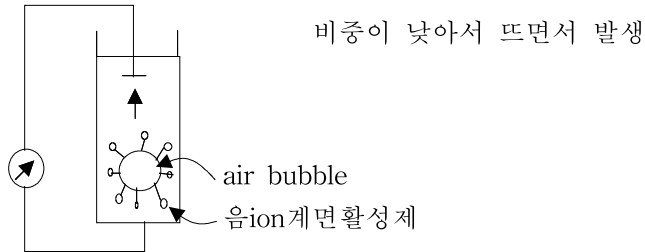
$\psi = 0$  at  $r = \infty$

$$\psi = \psi_0 \frac{R}{r} \exp(-K(r-R))$$

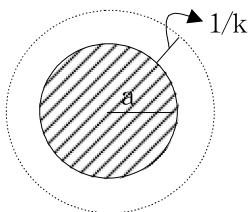
• Electro Kinetic Phenomena

- ① Electrophoresis(전기영동) : 주어진 외부전압하에서 전하를 띤 콜로이드 입자(무기, 유기, 고분자, 단백질)들이 움직이는 현상
- ② Electro-osmosis : 외부전압에 의하여 전하를 띤 표면을 따라 ion을 함유한 용액이 흐르는 현상

- ③ Streaming potential : stationary charged surface를 따라 ion을 함유한 유체를 흐르게 할때 발생하는 전압  
 ⇒강제로 흐르게 하면 potential생김
- ④ Sedimentation potential : charged particle을 액체내부에서 강제로 흐르게 할때 발생하는 전압



• Zeta-potential ( $\zeta$ -potential)



shear surface : 입자는 항상 유체층을 갖고 움직인다

shear surface의 potential을  $\zeta$ -potential이라 함

① Hukel Eq. ( $Ka \ll 1.0$ , non-conducting particle)

$$Ka = \frac{a}{\frac{1}{k}} = \text{입자의 반경 / (effective double layer thickness)}$$

a : 小

1/k : 大 ⇒ 입자size가 작고 천천히 drop

$$Q_E \cdot E = 6\pi\eta a V_E = F \text{ (by stoke's law)}$$

$Q_E$  : net charge of particle surface

E : electric field strength

$\eta$  : 용액의 점도

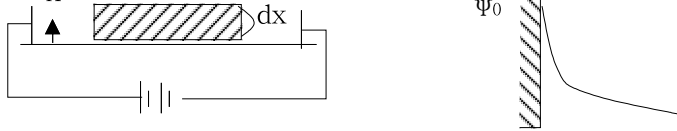
$V_E$  : 입자의 이동속도

$$u_E = \frac{V_E}{E} = \frac{QE}{6\pi\eta a} = \text{electrophoretic mobility}$$

$$\zeta = \frac{Q_E}{4\pi E a} - \frac{Q_E}{4\pi E(a + 1/k)} = \frac{Q_E}{4\pi E a(1 + ka)} \quad \text{if } Ka \ll 1.0 \text{ (대개 } 0.1\mu\text{m 이하 입자에겐 적용된다)}$$

$$\therefore u_E = \frac{4\pi E a \zeta}{6\pi \eta a} = \frac{\zeta E}{1.5\eta} \quad \text{입자 surface potential } \uparrow, \text{ 입자간 반발력도 } \downarrow$$

② Smoluchowski ( $Ka \gg 1.0$ , non-conducting particle)



plate로 가정

differential segment의 unitwidth에서 force balance

$$E\rho dx \cdot 1 = \left[ \eta \frac{dV}{dx} \right]_{x+dx} - \left[ \eta \frac{dV}{dx} \right]_x dx$$

$$\text{since } \rho = - \frac{d}{dx} \left[ E \frac{d\psi}{dx} \right] \quad -E \frac{d}{dx} \left[ E \frac{d\psi}{dx} \right] = \frac{d}{dx} \left[ \eta \frac{dV}{dx} \right]$$

$$\text{적분 } -EE \frac{d\psi}{dx} = \eta \frac{dV}{dx} + C_1 \quad (\because \text{at } x = \infty, \frac{d\psi}{dx} = \frac{dV}{dx} = 0)$$

$$\text{적분 } -EE\psi = \eta V + C_2 \quad \text{B.C. } \psi = 0, V = 0 \quad \text{at } x = \infty$$

$$\psi = \zeta, V = -V_E \quad \text{at shear surface}$$

$$-EE\psi = \eta V \quad \therefore u_E = \frac{V_E}{E} = \frac{\zeta E}{\eta}$$

③ Hery Eq. (for conducting as well as non-conducting particle)

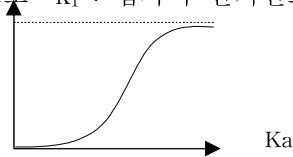
$$u_E = \frac{\zeta E}{1.5\eta} [1 + \lambda F(Ka)]$$

: 전도성이 아주 좋은 용액의 입자는 전기를 통해서도 입자 움직이지 않는다

$$\lambda = \frac{k_0 - k_1}{2k_0 + k_1} \quad k_0 : \text{용액의 전기전도도} \quad k_1 : \text{입자의 전기전도도}$$

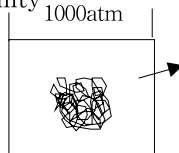
for non-conducting particle  $\lambda = 1/2$

if  $k_1 = \infty$  (전기전도도 high)  $\lambda = -1$



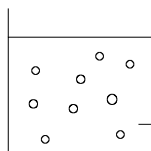
### Chap. 8. Colloidal Stability

① Sludge 처리



입자사이에  $H_2O$  : 80%  
Clay, 미생물 : 20%

② Polyester



homogeneous  
250°C melt  
실 뽑아냄

• Aggregate 형성

Driving force : vander waals' attractive force ( $V_A$ )

Against force electrostatic repulsive force ( $V_R$ )

steric hindrance by polymer

solvation force

• Critical coagulation concentration (CCC)

① salt : particle surface의 electrical property 변화  $\Rightarrow$  입자간  $V_R$ 이 변화

② CCC: colloid분산계에서 colloid입자들을 aggregation시키는데 필요한 salt의 농도

$$V_{total} = V_A + V_R$$

• Interaction Energy = van der waals' attractive interaction energy

- electrostatic repulsive energy

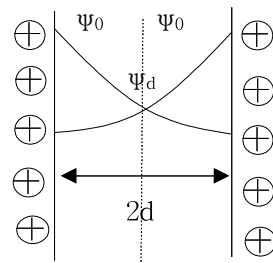
cf)  $\frac{dE}{dx} = F$        $w = Fdx = dE$

※ for flat plate

오른쪽 fixed, 왼쪽  $\leftarrow$  : 무한대거리로부터 2d거리까지

가져오는데 하는 일

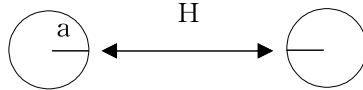
왼쪽 " , 오른쪽  $\rightarrow$  : " "



unit area

$$Gd = w = - \int_{\psi_d}^{\psi_\infty} \rho d\psi \quad \rho = ze(n^+ - n^-) \quad V_R = 2Gd$$

for spherical particle



$$V_R = 2\pi E \psi_d^2 \exp(-\kappa H)$$

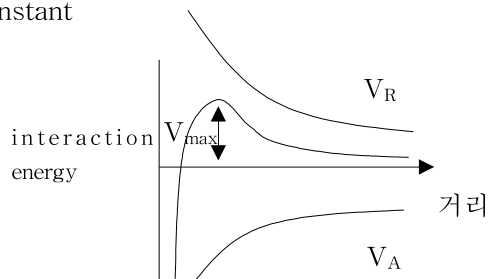
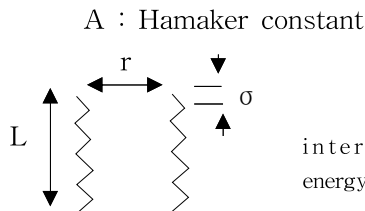
van der waals attractive energy

$$w = - \frac{c}{r^6}$$

$$V_A = - \frac{Aa}{12H}$$

polymer chain

$$V_A = - \frac{3\pi AL}{8\sigma^2 r^5}$$



$V_{max} > kT \Rightarrow$  stable dispersion

$V_{max} < kT \Rightarrow$  aggregation

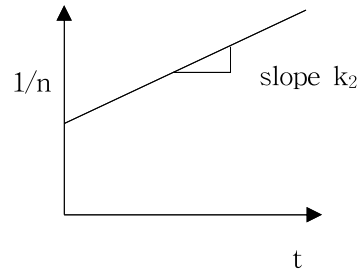
• Kinetics of coagulation

n : 단위부피당 입자수

$$-\frac{dn}{dt} = k_2 n \cdot n = k_2 n^2 \quad n = n_0 \quad \text{at} \quad t = 0$$

$$-\int_{n_0}^n \frac{dn}{n^2} = \int_0^t k_2 dt$$

$$1/n - 1/n_0 = k_2 t$$



※ Coulter counter

: 입자가 흐르면서 두 전극사이의 전류변화가 생김  
거기서 입자수 측정

• Systems containing lyophilic material

Solvation : solvent분자들이 입자표면에 흡착되어 한입자로 간주되는 현상

Hydration : solvent가 H<sub>2</sub>O인 경우

• Ion의 hydration ⇒ surface charge density에 비례

Bare ionic size : Li<sup>+</sup> < Na<sup>+</sup> < K<sup>+</sup> < Cs<sup>+</sup>

Surface charge density : Li<sup>+</sup> > Na<sup>+</sup> > K<sup>+</sup> > Cs<sup>+</sup>

Hydrated ionic size : Li<sup>+</sup> > Na<sup>+</sup> > K<sup>+</sup> > Cs<sup>+</sup>

※ 입자의 potential E ↓ ⇒ 쉽게 aggregate가 일어난다

• Salting-out : 용해된 물질이 salt의 첨가에 의하여 석출되는 현상

Salting-in : 석출된 물질이 salt의 첨가에 의하여 투명한 용액으로 다시 용해되는 현상

Salting-out power ⇒ Mg<sup>2+</sup> > Ca<sup>2+</sup> > Sr<sup>2+</sup> > Ba<sup>2+</sup> > Li<sup>+</sup> > Na<sup>+</sup> > K<sup>+</sup>

Salting-in ⇒ NH<sub>4</sub>NO<sub>3</sub>

Chap.9 Rheology

물질의 흐름과 변형을 다루는 학문

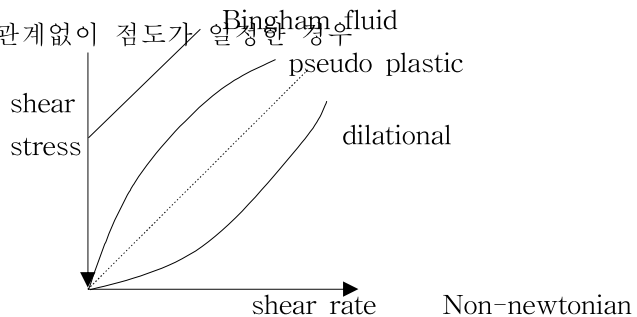
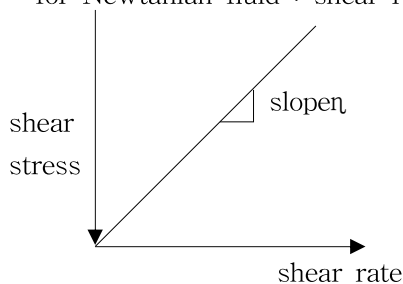
⇒ rubber, plastic, food, colloid용액

• Colloid system의 Rheology에 영향을 미치는 factor

- ① dispersion medium의 점도
- ② particle의 수
- ③ particle size, 모양
- ④ particle-particle 사이의 영향

• Viscosity : 흐름에 저항하는 정도

for Newtonian fluid : shear rate에 관계없이 점도가 일정한 경우



• Viscosity 측정

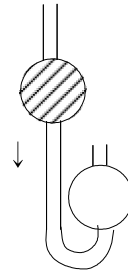
① Capillary flow method

$$\eta = \rho kt$$

$$\eta_1 = \rho_1 k t_1$$

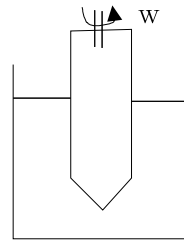
$$\eta_2 = \rho_2 k t_2$$

$$\therefore \frac{\eta_1}{\eta_2} = \frac{\rho_1 t_1}{\rho_2 t_2}$$



② Rotational method

$$\eta = \frac{k\theta}{w}$$



③ Cone-plate viscometer

$\eta_0$  : viscosity of dispersion medium

$\eta$  : colloid 용액의 점도

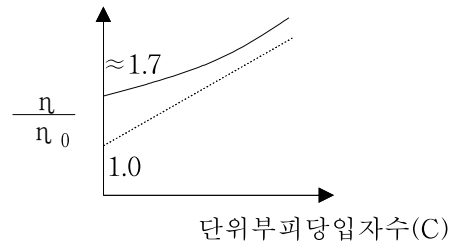
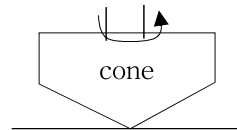
$$\frac{\eta}{\eta_0} = \text{relative viscosity}$$

$$\lim_{c \rightarrow 0} \frac{\eta}{\eta_0} = \text{intrinsic viscosity}$$

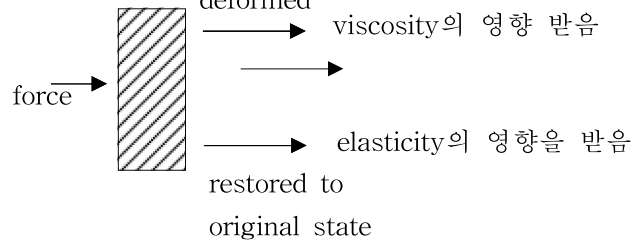
for spherical dilute colloidal system

$$\eta = \eta_0(1 + 2.5\Phi) \quad \Phi < 0.02 \text{인 경우}$$

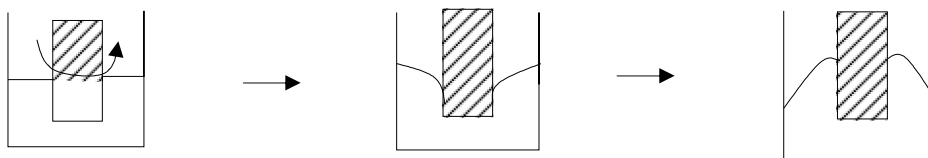
$$\Phi = \frac{\text{particle의부피}}{\text{medium의부피}}$$



• Viscoelasticity



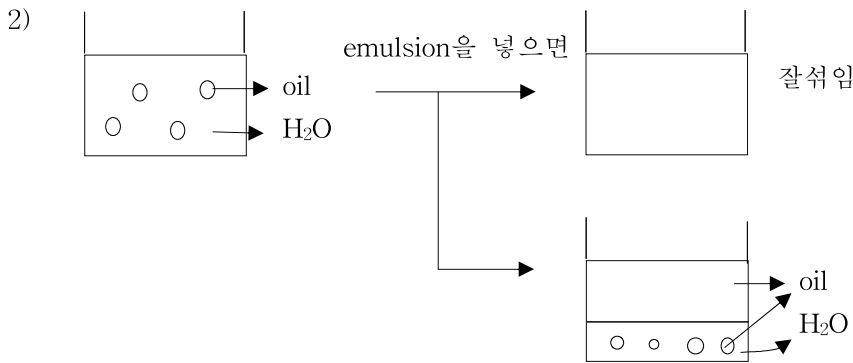
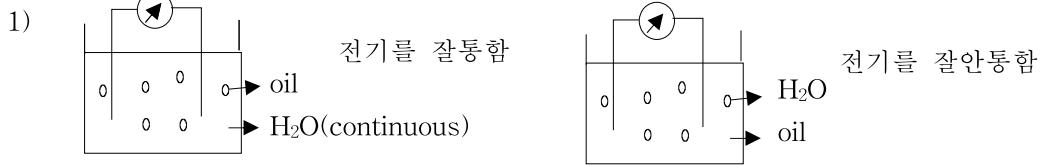
• Weissenburg Effect (polymer)



Chap 10. Emulsion & Foam

서로 섞이지 않는 유체들에서 하나의 유체가 다른 유체에 drop형태로 dispersion

• Methods to determine the structure of emulsion

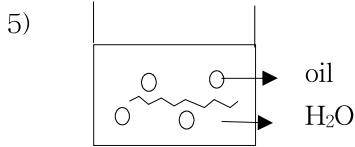


3)  $\eta = \eta_0(1 + 2.5\Phi)$

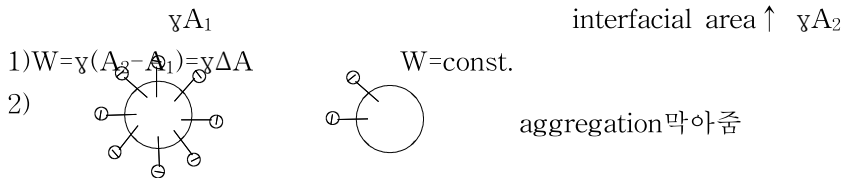
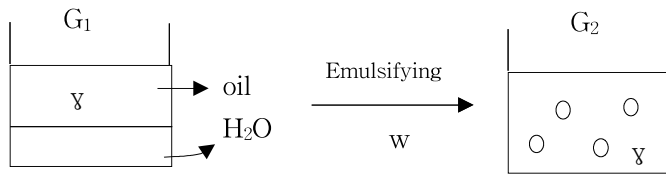
o/w ; oil첨가 점도 ↑, H<sub>2</sub>O첨가 점도 ↓

4) 수용성 dye하면 염색 good

ion성 " " bad



• Emulsifying Agents : variable, 섞어서 쓰기도 함



$G_1 < G_2$ 이므로 방향이 반대 방향으로 진행 ordinary solution

polymeric solution



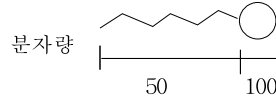
flocculation : 각각의 성질을 가지고 있다. low energy로도 분산가능

coagulation : 완전히 하나로 합쳐진 것. high energy가 필요

• HLB Number =  $\frac{\text{weight\% of 친수성 group}}{5}$

: 한분자내의 친유성과 친수성의 balance의 상대적 차이를 지수화

$$HLB = \frac{\frac{100}{150} \times 100}{5}$$



only 친수성 ; HLB=20

only 친유성 ; HLB=0

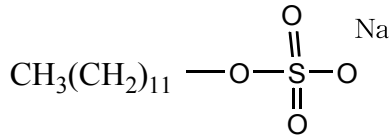
for nonionic HLB  $\updownarrow$  친유성, oil-soluble

20 친수성, water-soluble

for ionic

$$HLB = \sum(\text{hydrophilic number}) - \sum(\text{hydrophobic number}) + 7 \quad (0 \sim 40)$$

ex)



$$HLB = (-0.475) + (-0.475) \times 11 + 38.7 + 7$$

$$HLB_{\text{mixture}} = fHLB_A + (1-f)HLB_B \quad (f : A \text{의 mole fraction})$$

; 계면활성제는 보통 여러종류 섞어서 많이 사용

HLB values(Bancroft rule)

oil-soluble  $\Rightarrow$  w/o emulsion

water-soluble  $\Rightarrow$  o/w emulsion (oil in water)

• Emulsification Methods : w 가해주는 방법

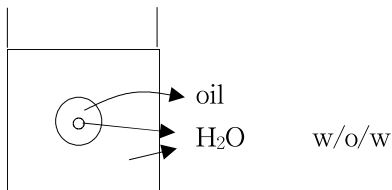
1) Homogenizer : high-speed mixer

2) Colloid mill

3) High pressure homogenizer

식품원료(물, 기름x)

• Multiple Emulsion



• Rheology of Emulsion

microstructure가 network형성 : 점도 ↑ for 생산성 cost control

• Application of Emulsion

- cola

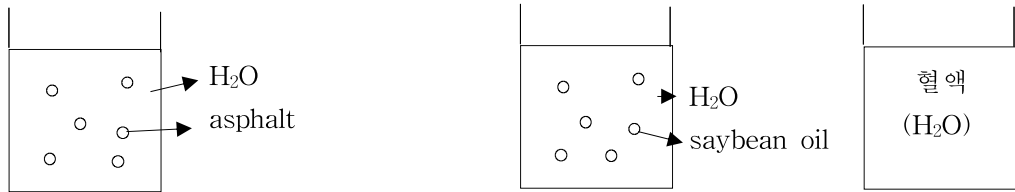
- paper wax coating

: candle 수용액내에 60°C에서 melting size 1μm로 분산

⇒ 이 emulsion을 종이에 발라서 물증발 시킴

- 아스팔트 : 점도 ↑

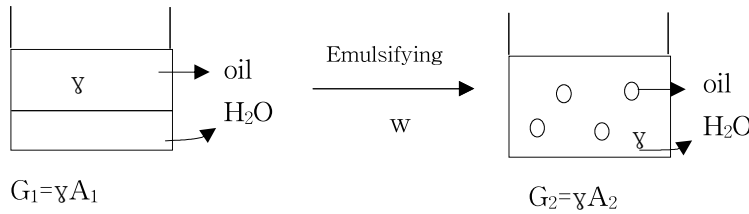
- medical and pharmaceutical



- Explosion : 단시간내에 다량의 gas생산 (압력 ↑)

• Microemulsion

Emulsion { microemulsion : drop size 0.1μm이하, 투명, 열역학적으로 stable  
 minienulsion  
 (macro)emulsion : 0.5μm이상, milky, 열역학적으로 unstable



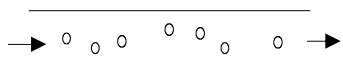
$\Delta G = \gamma(A_2 - A_1)$   $\gamma \approx 0$  (or negative)여야 0.1μm이하로 쪼개짐

∴ 열역학적으로 stable

emulsion인 경우  $\Delta G > 0$ 이므로 unstable

• Potential application of microemulsion

Soil



oil이 퍼져있는걸 모아주는 거

organic reaction

A와B가 서로 성질이 다를 때

