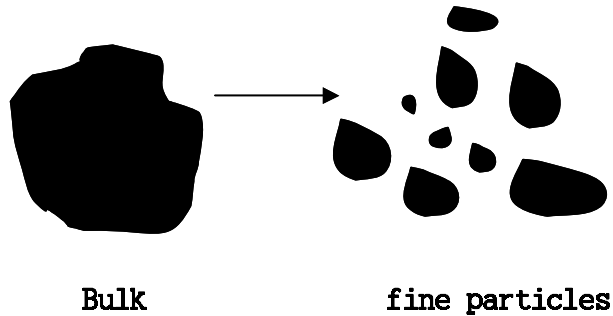


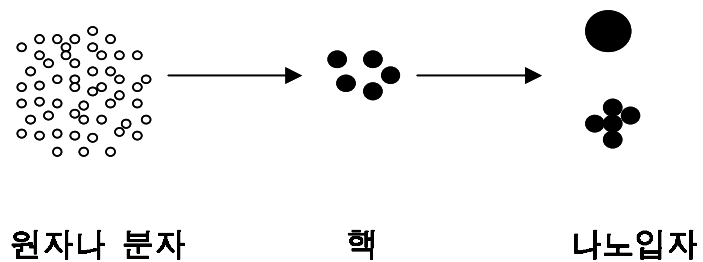
## Chapter 10. Particle Size Reduction

### \* Methods of Particle Production

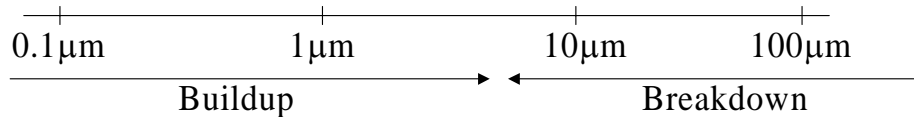
- Breakdown(Disintegration) : down to  $3\mu\text{m}$  (분쇄, 파쇄, 풍화, 분무)  
"3 $\mu\text{m}$ 의 벽"



- Buildup(Growth) : 핵생성 성장(응축, 응집)



\*



### 10.1 Introduction

- To create particles in a certain size and shape
- To increase the surface area available for next process
- To liberate valuable minerals held within particles

- \* Size reduction process : extremely energy-intensive
  - 5 % of all electricity generated is used in size reduction
  - Efficiency of size reduction : 1 %

## 10.2 Particle Failure Mechanisms

☞ <http://www.cpe.surrey.ac.uk/dptri/mg/impact.htm>

Stress-strain behavior

Interatomic force vs. interatomic distance

Figure 10.1

yield strength - tensile strength

brittle vs. ductile(tough)

Strain energy : energy stored in a body under tension

→ not uniform but concentrated in  
splits, cracks, hollow parts, foreign inclusions,  
displacement

Inglis (1913)

Stress concentration factor,  $K$

$$K \equiv \frac{\text{local stress}}{\text{mean stress in body}}$$

$$= 1 + 2\sqrt{L/R}$$

where  $L$  : half the length of the crack

$R$  : the radius of the crack tip or hole

Griffith (1921)

For crack to propagate

Strain energy > surface energy created

Requires appropriate crack propagation mechanism

\* Critical minimum crack length,  $L_c$

If  $L > L_c$ , the crack propagate

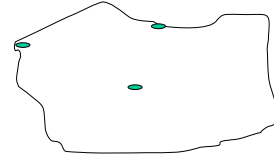
Dissipation velocity of excess strain energy = sonic

> crack propagation velocity → multiple fracture

Gilvary (1961)

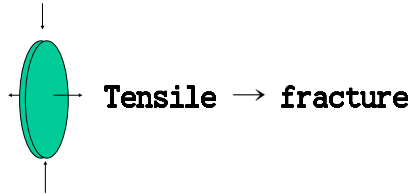
Volume, facial, edge cracks → different size distribution

size reduction



Evans(1961)

Compressive



\* For small particles

Needs more difficult to break,  $K \downarrow$

- Small L

- Less space for stress distribution → overestimate of K

e.g. Grindability limit

$4 \mu m$  for quartz

$1 \mu m$  for calcite

## 10.3 Models Predicting Energy Requirements and Product Size Reduction

### 1) Energy requirement for size reduction

Rittinger(1867)

$$E = C_R \left[ \frac{1}{d_{p2}} - \frac{1}{d_{p1}} \right] \text{ or } \frac{dE}{dd_p} = - C_R \frac{1}{d_p^2}$$

where  $d_{p1}$ ,  $d_{p2}$ : diameters of initial and final particles

$C_R$ : a constant

Kick(1885)

$$E = C_K \ln\left(\frac{d_{p1}}{d_{p2}}\right) \text{ or } \frac{dE}{dd_p} = C_K \frac{1}{d_p}$$

where  $C_K$ : a constant

Bond(1952)

$$E = C_B \left( \frac{1}{\sqrt{d_{p2}}} - \frac{1}{\sqrt{d_{p1}}} \right) \text{ or } \frac{dE}{dd_p} = C_B \frac{1}{d_p^{3/2}}$$

or

$$E_B = W_1 \left( \frac{10}{\sqrt{d_{p2}}} - \frac{10}{\sqrt{d_{p1}}} \right)$$

where  $d_{p1}$ ,  $d_{p2}$  : top particle sizes before and after, or  
the sieve sizes in  $\mu m$  through which 80%  
powders in the feed and product, respectively.

$W_1$  : Bond work index

e.g.  $W_1 = 9.45 \text{ kWh/ton}$  for bauxite  
= 20.7 for coke from coal  
= 8.16 for gypsum rock

In general,

$$\frac{dE}{dd_p} = -\frac{C}{d_p^N}$$

where  $N = 2$  for Rittinger  
= 1 for Kick  
= 1.5 for Bond

Figure 10.2

Kick  $\rightarrow$  Bond  $\rightarrow$  Rittinger as  $d_p \downarrow$

2) Prediction of the Product Size Distribution

## Definitions

$S_j$  : the specific rate of breakage

- probability of a particle of size  $j$  being broken in unit time

$b(i, j)$  : breakage distribution function

- fraction of size  $i$  from the breakage of mother particle  $j$

Then population balance:

$$\frac{dm_i}{dt} = \sum_{j=1}^{j=i-1} b(i, j) S_j m_j - S_i m_i$$

where  $i < j$

Figure 10.3

\*  $B(i, j)$ :  $j \rightarrow i$  to  $n$

In terms of mass fraction

$$\frac{dx_i}{dt} = \sum_{j=0}^{j=i-1} b(i, j) S_j x_j - S_i x_i$$

## **10.4 Types of Comminution Equipment**

### **1) Factors Affecting Choice of Machine**

- Stressing mechanism
- Mode of operation : batch/continuous or open/closed circuit
- Capacity
- Size of feed and product
- Material properties
- Carrier medium : air/inert gas/water/oil
- Integration with other unit operation : drying, classification, mixing, transportation, storage

### **2) Stressing Mechanisms**

Stressing between two solid surfaces : *Crushing*

Figure 10.4

- 0.01 - 10m/s
- For coarse(< 100mm) and medium-coarse size reduction (< 10mm)
- For medium-hard(Moh's:4-6) to medium materials(Moh's:7-10)

Jaw crusher(Figure 10.6)

Gyratory crusher(Figure 10.7)

Crushing roll(Figure 10.8)

Horizontal table mill(Figure 10.9)

Stressing against solid surface : *High velocity impact*

- Medium-fine to ultrafine comminution

Hammer mill(Figure 10.10)

Pin mill(Figure 10.11)

Fluid energy mill(Jet mill)(Figure 10.12)

Stressing by *Crushing and impact* (or using carrier medium)

Sand mill(Figure 10.13)

Colloid mill(Figure 10.14)

Ball mill(Figure 10.15)

\* Wet size reduction

- Stressing between two surfaces + shearing forces of the medium
- finer products/lowering dust emission/30% energy saving
- higher wear/needs wastewater treatment

### 3) Particle Size

Terminologies of comminution according to particle size

Table 10.1

*comminution equipment* according to particle size

Table 10.2

#### **4) Material Properties**

- Hardness(opposite of abrasiveness):If low, use low-speed mill
- Toughness: lowering temperature cf. brittleness
- Co-Adhesivity: wet grinding
- Fibrous nature: with shredders and cutters
- Low melting point: with cold air
- Thermally sensitive materials, flammability: with inert  
carrier medium
- Toxic/radioactive materials: closed circuit

\* Mechanochemistry

#### **5) Carrier Medium**

Gas

Liquid(water, oil)

Powder transportation

Control of force transmission, friction, abrasion, crack, co- or  
adhesivity, electrostatic charging, flammability,

#### **6) Modes of operation**

Batch vs. continuous

#### **7) Combination of Other Operation**

Drying, mixing or classification

#### **8) Types of Milling Circuits**

Open circuit vs. closed circuit

Figure 10.16      Figure 10.17, 10.18