



Turbidostat Response (TURBCON)



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Model

- Schematic diagram

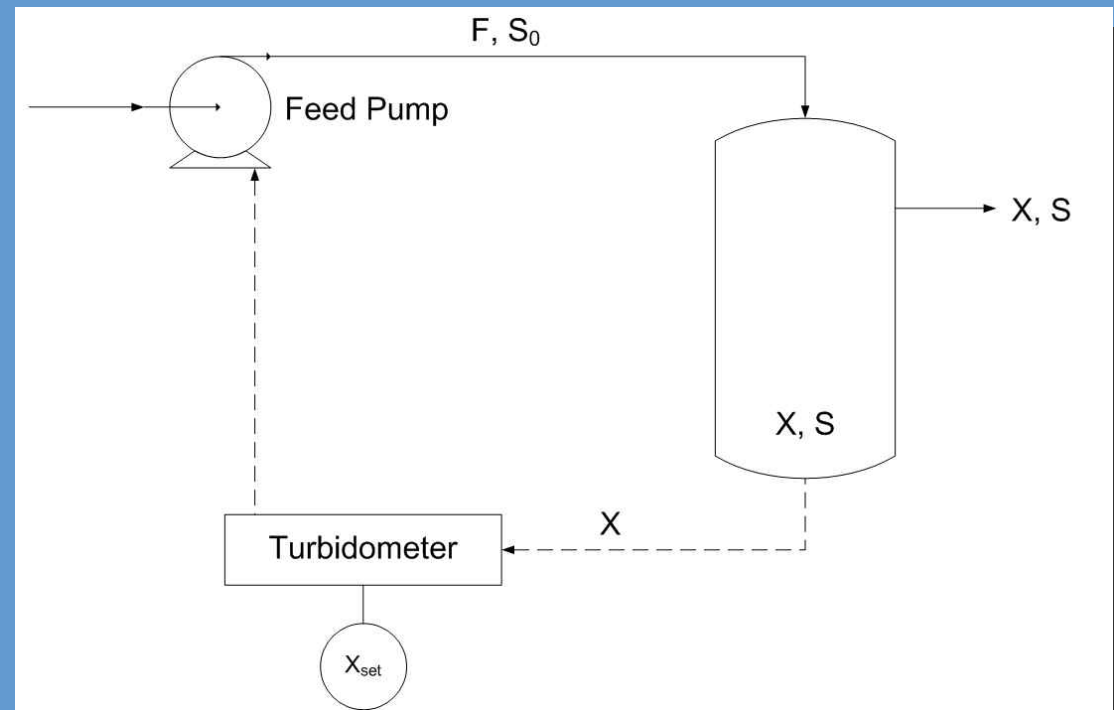


Fig. 1. Feedback control of the biomass concentration using a Turbidostat.



Model

- For the well-mixed tank with Monod growth

$$\mu = \frac{\mu_m S}{K_s + S}$$

$$\frac{dS}{dt} = \frac{F(S_0 - S)}{V} - \frac{\mu X}{Y}$$

$$\frac{dX}{dt} = -\frac{FX}{V} + \mu X$$

- Luedeking-Piret kinetics

$$\frac{dP}{dt} = -\frac{FP}{V} + (B + \mu A)X$$

- PI control

$$F = F_0 + K_p \varepsilon + \frac{K_p}{\tau_I} \int \varepsilon dt$$

$$\varepsilon = (X - X_{set})$$



Model



Symbols

A	Growth-associated constant	-
B	Nongrowth-associated constant	1/h
F	Flow rate	m ³ /h
F ₀	Normal feed flow rate	m ³ /h
K _p	Proportional controller constant	m ⁶ /(h·kg)
K _s	Saturation constant	Kg/m ³
P	Product concentration	Kg/m ³
S	Substrate concentration	Kg/m ³
V	Reactor Volume	m ³
X	Biomass concentration	Kg/m ³
Y	Yield coefficient	Kg /kg
τ _i	Integral control time constant	h

Indices

m	Refers to maximum
P	Refers to proportional control
S and set	Refers to setpoint
0	Refers to inlet stream



Programming Source



M-file

```
• function dydt=TURBCON(t,y)
• clc;
• UM=0.5; KS=0.1;      Y=0.8;
• V=1;   S0=5;        TI=10;      %Constant
• F0=0.2;  KP=0.25;   A=0.2;
• B=0.15;  XS=2.0;
• if (y(2)<0)
•     y(2)=0;
•     end;
• U=UM*y(2)/(KS+y(2));
• E=y(1)-XS;          % Error
• F=F0+KP*E+KP/TI*E*t;
• y1=y(1);            % y1=X
• y2=y(2);            % y2=S
• y3=y(3);            % y3=P
• dydt=[-F*y(1)/V+U*y(1);
•       F*(S0-y(2))/V-U*y(1)/Y;
•       -F*y(3)/V+A*U*y(1)+B*y(1)];
```

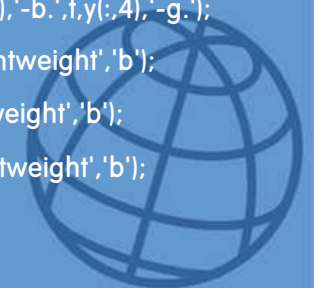
Command

```
• y0=[1,5,1];
• t0=0;tf=20.0;
• [t,y]=ode45('TURBCON',t0:0.01:tf,y0);
• plot(t,y(:,1),'-r.',t,y(:,2),'-k.',t,y(:,3),'-b.');
```

• title('TURBCON','fontsize',16,'fontweight','b');
• xlabel('TIME','fontsize',12,'fontweight','b');
• ylabel('X,S,P','fontsize',12,'fontweight','b');
• h=legend('X','S','P',0);
• set(h,'fontsize',8);

```
• y0=[1,5,1,0.2];
• t0=0;tf=40.0;
• [t,y]=ode45('TURBCON',t0:0.01:tf,y0);
• plot(t,y(:,1),'-r.',t,y(:,2),'-k.',t,y(:,3),'-b.',t,y(:,4),'-g.');
```

• title('TURBCON','fontsize',16,'fontweight','b');
• xlabel('TIME','fontsize',12,'fontweight','b');
• ylabel('X,S,P,F','fontsize',12,'fontweight','b');
• h=legend('X','S','P','F',0);
• set(h,'fontsize',8);



Matlab Programming

- M-file

```
MATLAB Editor/Debugger - [C:\MATLAB\bin\TURBCC
File Edit View Debug Window Help
function dydt=TURBCON(t,y)
clc;
UM=0.5;   KS=0.1;   Y=0.8;
V=1;     S0=5;     TI=10;   %Constant
F0=0.2;  KP=0.25;  A=0.2;
B=0.15;  XS=2.0;
if (y(2)<0)
    y(2)=0;
end;
U=UM*y(2)/(KS+y(2));
E=y(1)-XS;   % Error
F=F0+KP*E+KP/TI*E*t;
y1=y(1);    % y1=X
y2=y(2);    % y2=S
y3=y(3);    % y3=P
dydt=[-F*y(1)/V+U*y(1);
      F*(S0-y(2))/V-U*y(1)/Y;
      -F*y(3)/V+A*U*y(1)+B*y(1)];
```

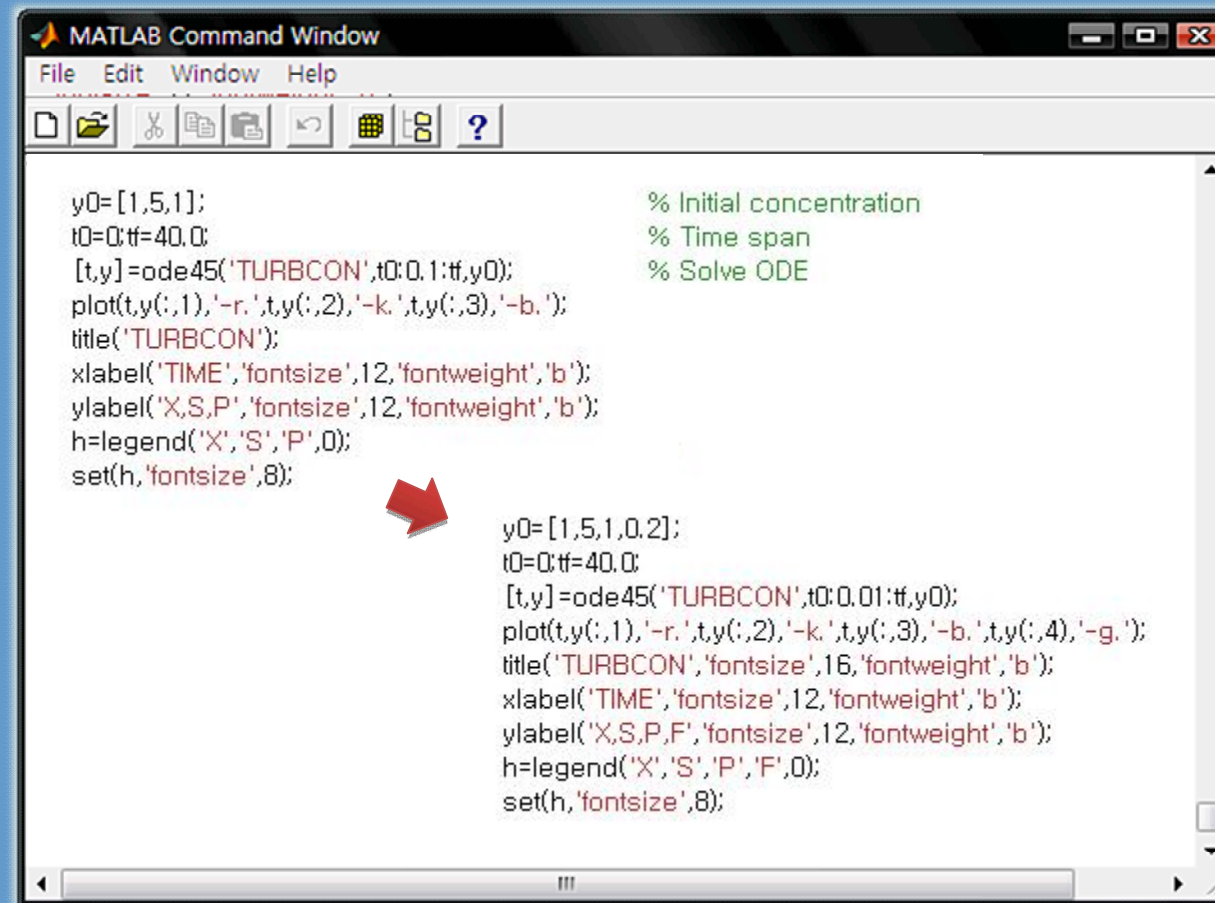


```
MATLAB Editor/Debugger - [C:\MATLAB...
File Edit View Debug Window Help
function dydt=TURBCON(t,y)
clc;
UM=0.5;   KS=0.1;   Y=0.8;
V=1;     S0=5;     TI=10;   %Constant
F0=0.2;  KP=0.25;  A=0.2;
B=0.15;  XS=2.0;
if (y(2)<0)
    y(2)=0;
end;
U=UM*y(2)/(KS+y(2));
E=y(1)-XS;   % Error
DX=-y(4)+y(1)/V+U*y(1);
y1=y(1);    % y1=X
y2=y(2);    % y2=S
y3=y(3);    % y3=P
y4=y(4);    % y4=F
dydt=[-y(4)+y(1)/V+U*y(1);
      y(4)+(S0-y(2))/V-U*y(1)/Y;
      -y(4)+y(3)/V+A*U*y(1)+B*y(1);
      KP*DX+KP/TI*E];
```



Matlab Programming

- Command



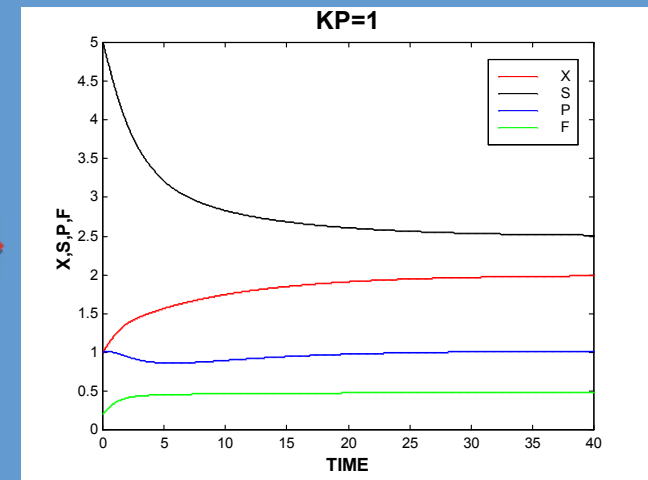
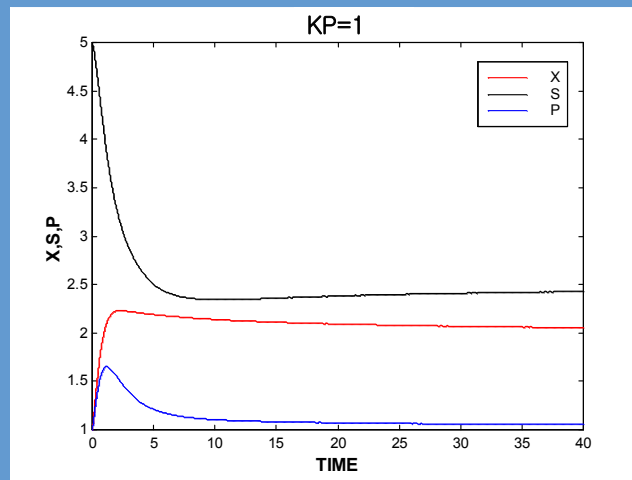
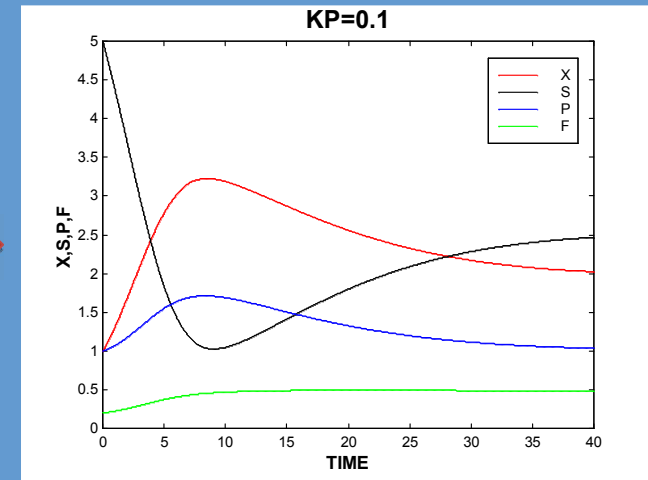
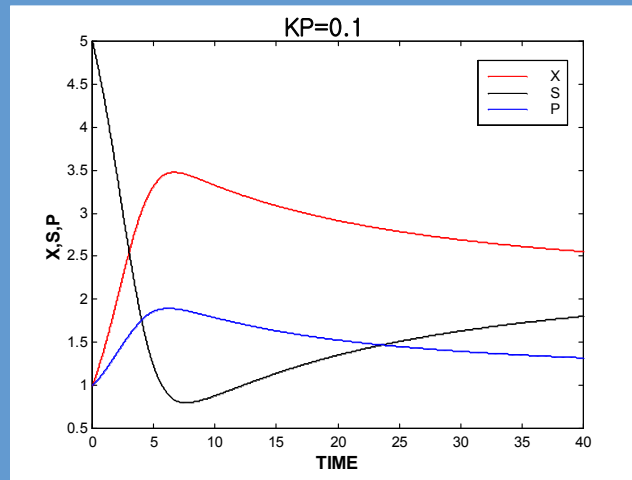
```
MATLAB Command Window
File Edit Window Help
[Icons]
y0=[1,5,1]; % Initial concentration
t0=0;tf=40.0; % Time span
[t,y]=ode45('TURBCON',t0:0.1:tf,y0); % Solve ODE
plot(t,y(:,1),'-r',t,y(:,2),'-k',t,y(:,3),'-b. ');
title('TURBCON');
xlabel('TIME','fontsize',12,'fontweight','b');
ylabel('X,S,P','fontsize',12,'fontweight','b');
h=legend('X','S','P',0);
set(h,'fontsize',8);

y0=[1,5,1,0.2];
t0=0;tf=40.0;
[t,y]=ode45('TURBCON',t0:0.01:tf,y0);
plot(t,y(:,1),'-r',t,y(:,2),'-k',t,y(:,3),'-b.',t,y(:,4),'-g. ');
title('TURBCON','fontsize',16,'fontweight','b');
xlabel('TIME','fontsize',12,'fontweight','b');
ylabel('X,S,P,F','fontsize',12,'fontweight','b');
h=legend('X','S','P','F',0);
set(h,'fontsize',8);
```



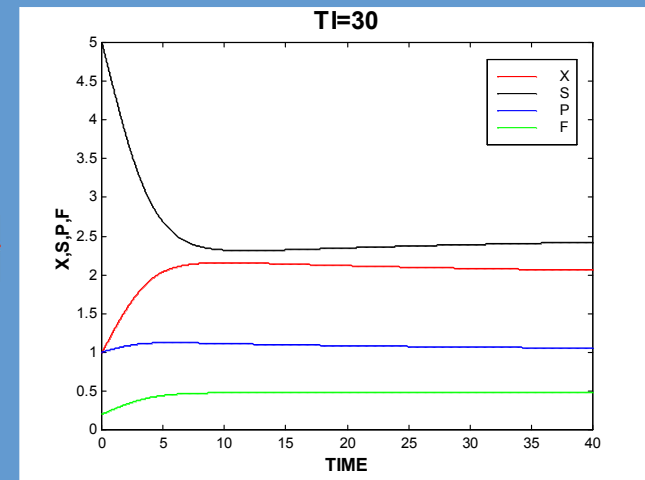
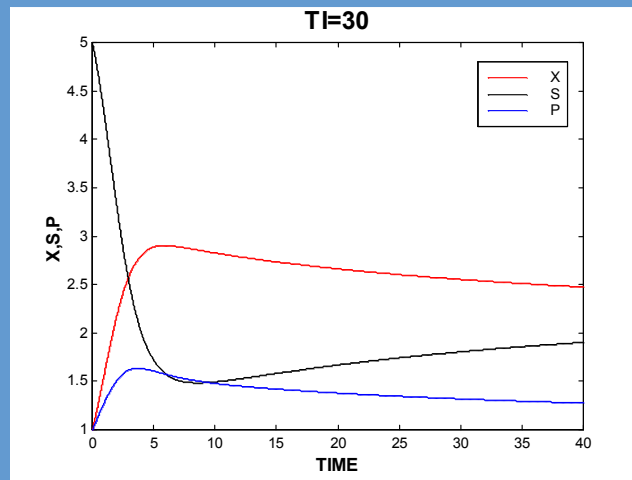
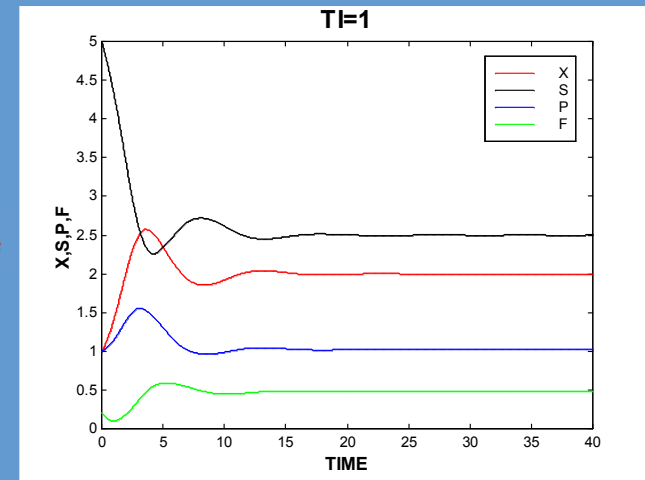
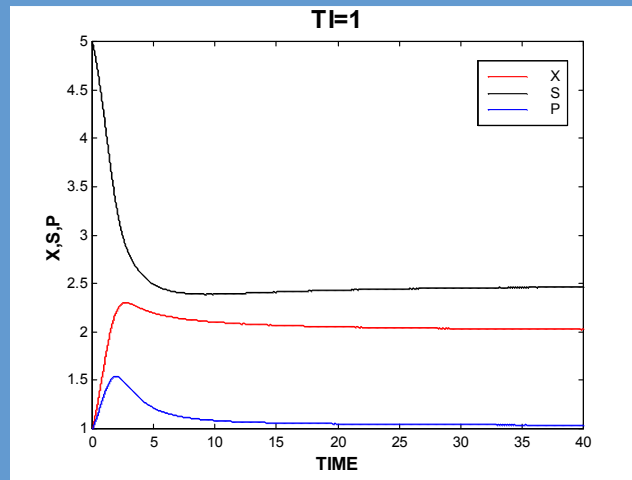
Changing Parameters

- Set K_p in the range 0.1 to 1



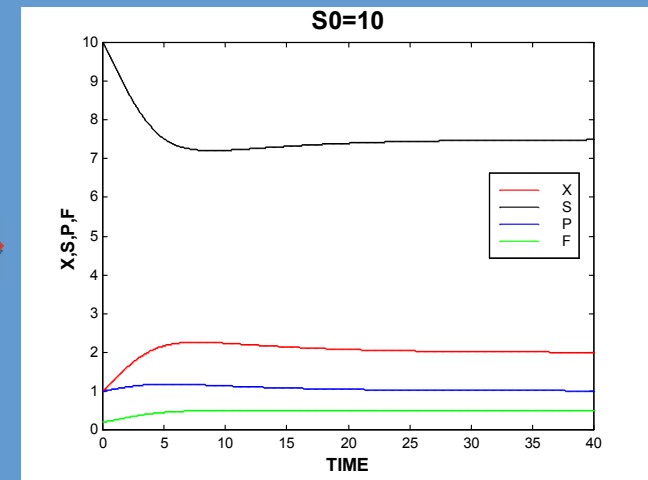
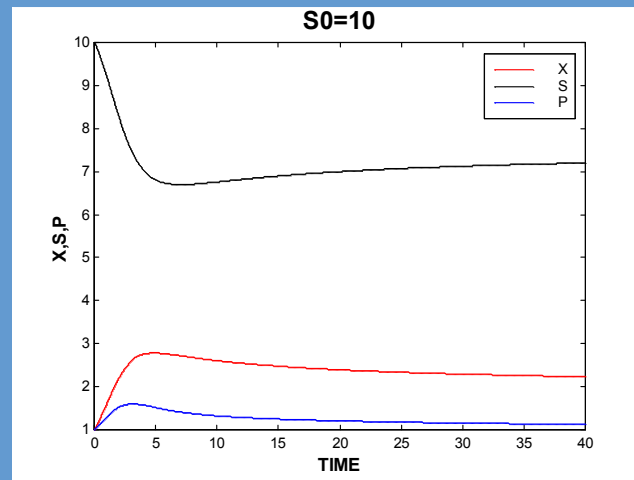
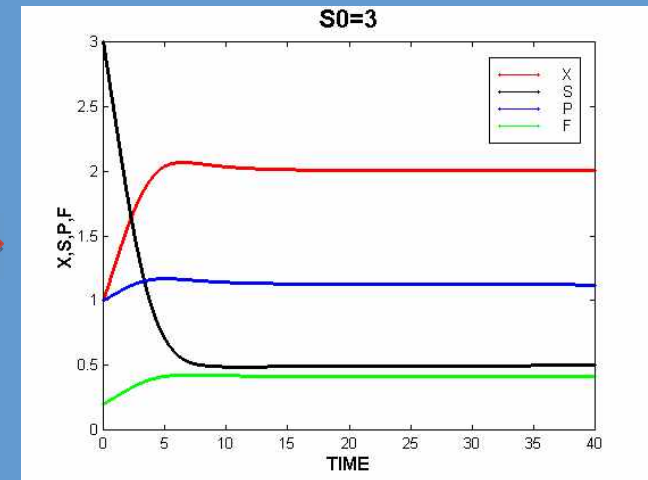
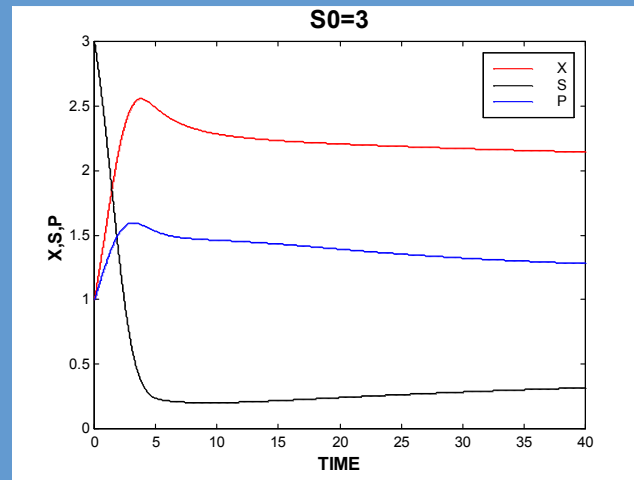
Changing Parameters

- Vary τ_1 in the range 1 to 30



Changing Parameters

- Vary S_0 in the range 3 to 10



Conclusion



- K_p 의 값이 클수록, τ 값이 작을 수록 최종값에 빨리 도달한다.
- S_0 의 양이 많아질수록 반응 용기의 기질의 농도는 증가하나 생성물 농도 (P)와 생장 농도 (X) 변화에는 거의 영향을 미치지 않는다.

