Chapter 9. Agitation and Mixing of Liquids

Agitation (교반): the induced motion of a material in a circulatory pattern

Mixing (혼합): the random distribution of two or more separate phases

→ 원래 정의는 다르지만 많은 경우 혼용해서 사용

Purposes of agitation:

Suspending solid particles (suspension)

Blending miscible liquids (alcohol & water)

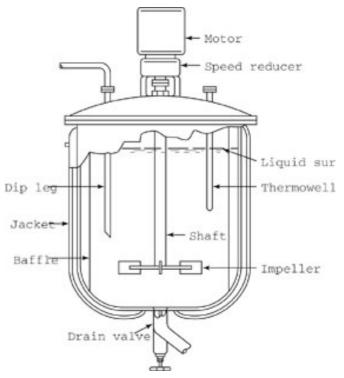
Dispersing a gas through the liquid (bubble)

Dispersing immiscible liquids (emulsion)

Promoting heat transfer

Agitated Vessels

: cylindrical form, vertical axis, closed or open top round bottom, equal liquid depth & tank diameter



Typical agitation process vessel



* Impellers

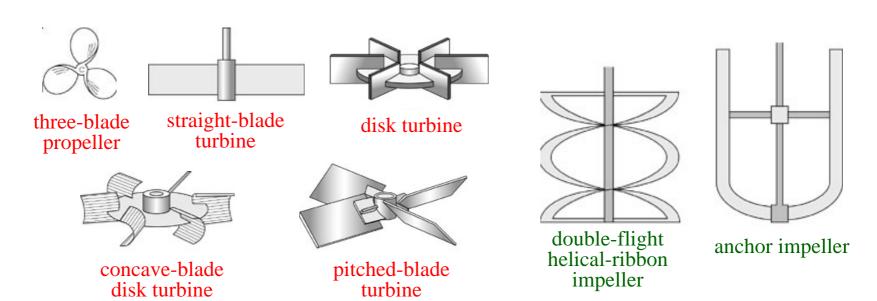
· Axial-flow impellers (축류 임펠러) · Radial-flow impellers (방사류 임펠러)

Impellers for low- to moderate- viscosity liquids:

propellers, turbines & high efficiency impellers

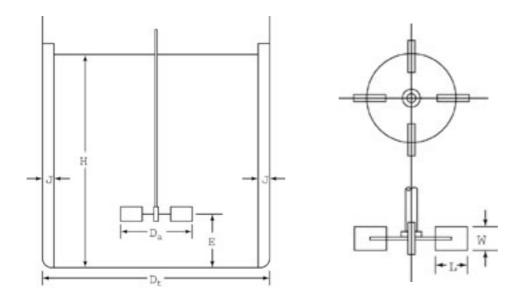
Impellers for very viscous liquids:

helical impellers & anchor agitators





Standard turbine design



H: depth of liquid

 D_t : tank diameter

 D_a : impeller diameter

 \boldsymbol{L} : blade length

W: impeller width

J: width of baffle

E: clearance

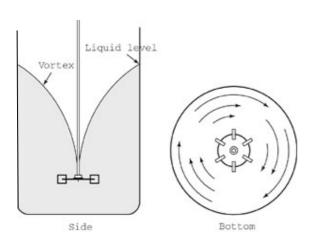
Typical proportions:

$$\frac{D_a}{D_t} = \frac{1}{3}$$
 $\frac{H}{D_t} = 1$ $\frac{J}{D_t} = \frac{1}{12}$ $\frac{E}{D_t} = \frac{1}{3}$ $\frac{W}{D_a} = \frac{1}{5}$ $\frac{L}{D_a} = \frac{1}{4}$

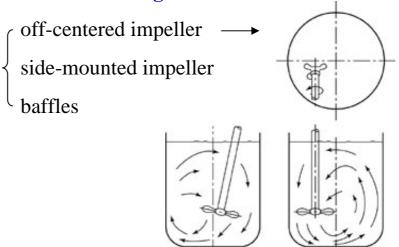
& No. of baffles: 4, No. of impeller blades: 6 or 8



Swirling flow pattern



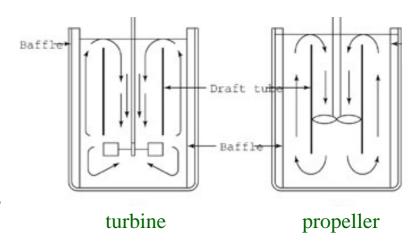
Prevention of swirling



Draft tubes

Controls direction and velocity of flow

Useful when high shear is desired such as emulsions and suspensions



Draft tubes, baffled tank

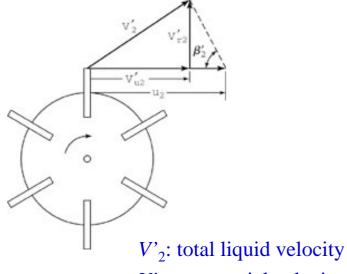


* Circulation rates

Large impellers at medium speed → promotes flow

Smaller impellers at high speed → generates intense turbulence

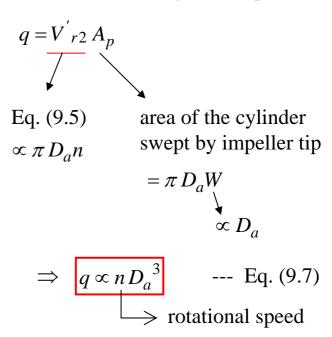
Flow number, N_O



 V_{u2} : total figure velocity V_{u2} : tangential velocity V_{r2} : radial velocity

 u_2 : blade tip velocity

Volumetric flow rate through the impeller





The rate of these two quantities \rightarrow Flow number, N_O

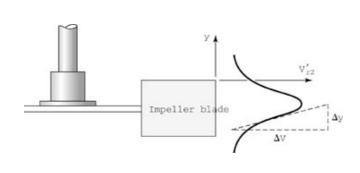
$$N_Q = \frac{q}{nD_a^{3}}$$
 --- Eq. (9.8)

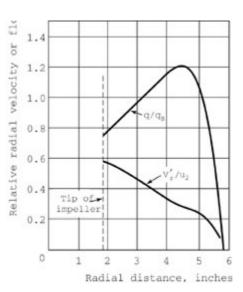
For a disk turbine: $N_Q=1.3$

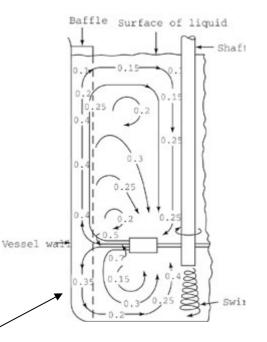
For marine propellers: N_Q =0.5

For a four-blade 45° turbine: N_Q =0.87

* Velocity patterns







Velocity profile and patterns in turbine agitator

Numbers indicate fractions of the velocity of the blade tip.



Tank Reynolds number, Re:

At Re < 10, laminar flow

At $Re > 10^4$, turbulent flow

* Power consumption

Power P: product of the flow rate q and the kinetic energy per unit volume E_k

$$q = nD_a^3 N_Q \qquad E_k = \frac{\rho(V_2')^2}{2}$$

$$\longleftarrow V_2' = \alpha u_2 = \alpha \pi n D_a$$

$$P = nD_a^3 N_Q \frac{\rho(\alpha \pi n D_a)^2}{2}$$
$$= \rho n^3 D_a^5 \left(\frac{\alpha^2 \pi^2}{2} N_Q\right)$$



이를 무차원 형태(dimensionless form)로 고쳐 표현하면,

$$\frac{P}{n^3 D_a^{5} \rho} = \frac{\alpha^2 \pi^2}{2} N_Q \qquad --- \text{ Eq. (9.11)}$$

윗 식에서 좌변 항을 Power number (동력수)로 정의함.

Power number, N_P :

$$N_P \equiv \frac{P}{n^3 D_a^{5} \rho}$$
 --- Eq. (9.12a)

: ratio of drag force to momentum flow N_P is analogous to f or C_D

즉, N_p 가 크면 동력소비가 큼.

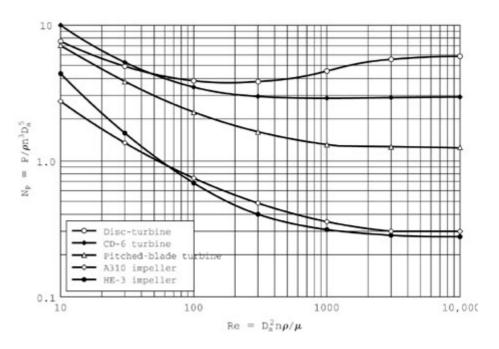


Fig. 9.13 Plots of power number N_P vs. Reynolds number Re for baffled tanks



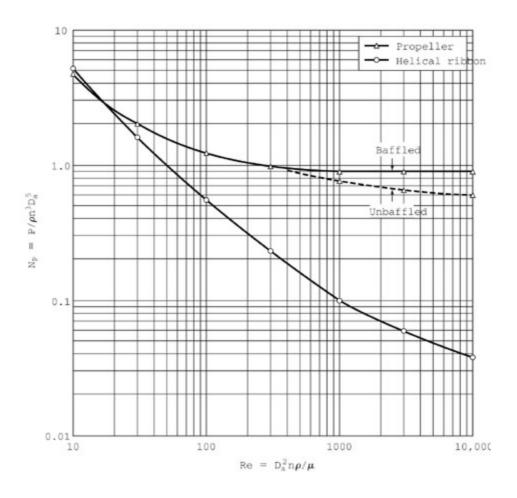


Fig. 9.14 Plots of power number N_P vs. Reynolds number Re for propellers and helical ribbons



Effect of system geometry

$$\cdot \quad \frac{D_a}{D_t} \downarrow \quad \longrightarrow \quad \left\{ \begin{array}{c} N_P \uparrow & \text{when baffles are few \& narrow} \\ N_P \downarrow & \text{when} & \text{many \& wide} \end{array} \right.$$

$$\cdot \quad \frac{E}{D_t} \uparrow \quad \longrightarrow \quad \left\{ \begin{array}{c} N_P \uparrow \text{ for a disk turbine} \\ N_P \downarrow \text{ for a pitched-blade turbine} \end{array} \right.$$

· Two turbines on the same shaft

$$\longrightarrow \begin{cases} 1.9 \text{ times power of one turbine when the spacing is longer than } D_a \\ 2.4 \text{ times} & \text{for closely spaced turbines} \end{cases}$$

• The shape of tank: little effect on N_P



Calculation of power consumption

The power delivered to the liquid,

$$P = N_P n^3 D_a^{\ 5} \rho$$
 --- Eq. (9.18) \leftarrow from Eq. (9.12a)
At low Re (Re < 10), $N_P = \frac{P}{n^3 D_a^{\ 5} \rho}$

$$N_P = \frac{K_L}{\text{Re}}$$
 for both baffled & unbaffled tanks

$$\therefore P = K_L n^2 D_a^{\ 3} \mu$$
 --- Eq. (9.20) . 상수 $K_L \& K_T$: Table 9.2 (또는 Figs. 9.13-14에서 N_P 값으로 제공)

At high Re (Re > 10,000),

$$N_P \neq ftn$$
 (Re) for baffled tanks
= K_T

:.
$$P = K_T n^3 D_a^{5} \rho$$
 --- Eq. (9.22)

 \leftarrow μ is not a factor



Ex. 9.1) A disk turbine with 6 blades in a baffled tank 2 m in diameter

Turbine diameter of 0.67 m positioned 0.67 m above the tank bottom

Turbine blade width of 134 mm, A depth of 2 m with 50% NaOH solution

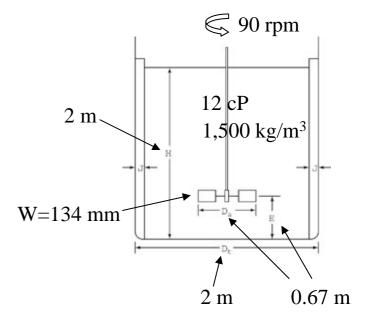
Viscosity of 12 cP, Density of 1,500 kg/m³, Impeller speed of 90 rpm

What power will be required?

Ans.)

Re =
$$\frac{nD_a^2 \rho}{\mu}$$
 = $\frac{1.5(0.67)^2 1500}{0.012}$ $\approx 84,169$

Re >10,000 이므로 $N_P = K_T$ 사용 Table 9.2에서 $K_T = 5.75$ Eq. (9.22)에서 계산하면,





Ex. 9.2) A disk turbine with 6 blades in a baffled tank 2 m in diameter

Turbine diameter of 0.67 m positioned 0.67 m above the tank bottom

Turbine blade width of 134 mm, A depth of 2 m with a rubber-latex compound

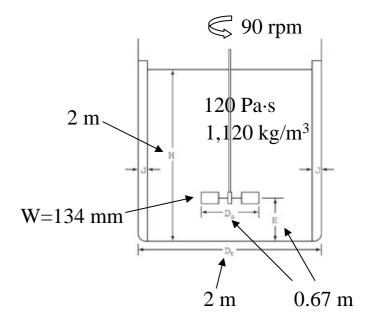
Viscosity of 120 Pa·s, Density of 1,120 kg/m³, Impeller speed of 90 rpm

What power will be required?

Ans.)

Re =
$$\frac{nD_a^2 \rho}{\mu}$$
 = $\frac{1.5(0.67)^2 1120}{120}$ ≈ 6.3

Re <10 이므로 N_P = K_L /Re 사용 Table 9.2에서 K_L =65 Eq. (9.20)에서 계산하면,





Blending and Mixing

Mixing time (혼합시간) t_T : the time to reach complete mixing (99% mixing)

achieved if the contents of the tank are circulated about 5 times

$$t_T \approx \frac{5V}{q_T}$$



 nt_T vs. Re

(Reynolds 수에 따른 혼합시간)

V: liquid volume in tank q_T : total liquid flow rate n: rotational speed (r/s)

ex) For turbine in a baffled tank with $D_d/D_t=1/3$, $D_t/D_H=1$ $\rightarrow nt_T=36$ for Re > 2,000

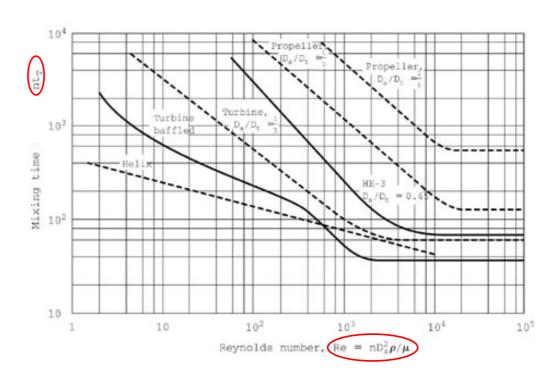


Fig. 9.16. Mixing times in agitated vessels. Dashed lines for unbaffled tanks; Solid lines for baffled tanks.



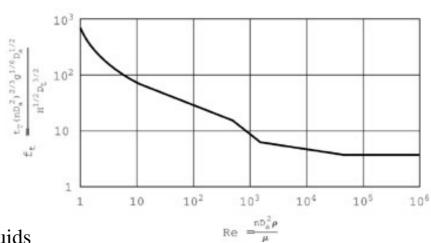
Mixing time factor (혼합시간 인자) f_t

A general correlation for turbines:

$$f_t = nt_T \left(\frac{D_a}{D_t}\right)^2 \left(\frac{D_t}{H}\right)^{1/2} \left(\frac{g}{n^2 D_a}\right)^{1/6}$$

A helical ribbon agitator:

shorter mixing times with very viscous liquids



In a pseudoplastic liquid: blending time is much longer than in Newtonian liquids.

Ex. 9.3) $D_t = 6$ ft (1.83 m), 6-straight blade turbine, $D_a = 2$ ft (0.61 m), $E = D_a$, n = 80 rpm, $H = D_t$ For neutralizing a NaOH solution with HNO₃ solution at 70 °F, $t_T = ?$

Ans.) From Appendix 6
$$\Rightarrow \rho = 62.30 \text{ lb/ft}^3 = 62.30 (0.453 \text{kg/lb}) (\text{ft/0.305m})^3 = 997 \text{kg/m}^3$$

 $\mu = 0.982 \text{cP} = 9.82 \times 10^{-4} \text{Pa} \cdot \text{s}$

:. Re =
$$\frac{nD_a^2 \rho}{\mu}$$
 = 503,000

From Fig. 9.16 for Re = 503,000,
$$nt_T = 36$$
 \rightarrow $t_T = 36/1.333 = 27s$



Dispersion Operations

Volume (or holdup) of dispersed phase Ψ

$$\Psi = \frac{\pi N D_p^3}{6}$$

 $\Psi = \frac{\pi N D_p^{3}}{N}$ N: the number of drops or bubbles per total volume

Total surface area of drops per total volume *a*

$$a = \pi N D_p^2$$
 \longrightarrow $D_p = \frac{6\Psi}{a}$ (실제로는 입자의 크기가 다르므로 평균입자경으로 정의)

Sauter mean diameter \overline{D}_s (or volume-surface mean diameter D_{32}) $\overline{D}_s = \frac{6\Psi}{a}$

$$\overline{D}_s \equiv \frac{6\Psi}{a}$$

* Liquid/liquid dispersion

Weber number
$$We$$

$$We = \frac{\rho_c (nD_a)^2}{\sigma/D_a} = \frac{\rho_c n^2 D_a^3}{\sigma}$$
: kinetic energy/surface energy

density of continuous phase

interfacial tension

$$\overline{D}_s/D_a \propto We^{-0.6} \longrightarrow We \uparrow \rightarrow \overline{D}_s \downarrow$$

Related problems: (Probs.) 9.1, 9.3, 9.5, 9.11(a) and 9.18

