

## Comprehensive Comparison and Evaluation of the WS, MHV2, Twu and CWSM Mixing Rules

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Three mixing rules, the Wong-Sandler (WS), MHV2, and Twu et al. (1991), are widely used for their predictive and correlative capability for VLE of highly non-ideal systems. Recently, a new mixing rule, the combined WS-Michelsen (CWSM) mixing rule has been proposed by the authors (Qu and Wang, 1995). It has been proved that the CWSM mixing rule is a good improvement over the WS mixing rule in complete predictions of VLE using the EoS/UNIFAC method. In this presentation, comprehensive comparison and evaluation have been conducted in terms of the PR EOS and experimental data for nonpolar-nonpolar, polar-polar and polar-nonpolar systems (see Table 1):

(1) Using the four mixing rules incorporated with the Wilson, UNIQUAC, NRTL activity coefficient models, VLE data at low and high pressures have been correlated. Correlated accuracies for the four mixing rules have been compared in Table 2.

(2) The WS, MHV2, CWSM mixing rules have been used to predict VLE at high pressures from the data at low pressures. Their predictive results have been compared in Table 3. In conclusion, of simplicity, the CWSM mixing rule presents the same quality correlation and better predictive results, in particular for asymmetric polar-nonpolar systems.

### References:

- Twu, C. H. et al., *Fluid Phase Equilibria*, 69: 33-50 (1991).
- Qu, Y. and W. Wang, A predictive equation of state/UNIFAC method for vapor-liquid equilibria, submitted to *Fluid Phase Equilibria*, March, 1995.

Table 1 Source of High-Pressure Experimental Data

System	n.d.*	Temp.(K)	Press.(Bar)	Ref.
1. Nonpolar - Nonpolar System				
A C <sub>2</sub> H <sub>6</sub> - C <sub>6</sub> H <sub>6</sub>	80	273.15 - 533.15	20.684 - 82.736	[11]
B C <sub>3</sub> H <sub>8</sub> - n-C <sub>6</sub> H <sub>14</sub>	40	333.15 - 493.15	0.763 - 41.368	[12]
C 1-C <sub>4</sub> H <sub>8</sub> - n-C <sub>4</sub> H <sub>10</sub>	33	310.93 - 338.71	3.551 - 8.693	[13]
D n-C <sub>4</sub> H <sub>10</sub> - n-C <sub>7</sub> H <sub>16</sub>	41	355.37 - 538.71	6.895 - 39.645	[14]
E n-C <sub>5</sub> H <sub>12</sub> - n-C <sub>7</sub> H <sub>16</sub>	28	403.75 - 526.45	10.132 - 30.610	[15]
2. Polar - Polar System				
F CH <sub>3</sub> OH - H <sub>2</sub> O	47	373.15 - 523.15	1.041 - 68.552	[16]
G C <sub>2</sub> H <sub>5</sub> OH - H <sub>2</sub> O	63	423.15 - 623.15	5.586 - 189.793	[17]
H 2-C <sub>3</sub> H <sub>5</sub> OH - H <sub>2</sub> O	93	298.15 - 355.54	0.032 - 9.170	[18]
I C <sub>3</sub> H <sub>6</sub> CO - H <sub>2</sub> O	91	298.15 - 523.15	0.067 - 67.586	[19]
3. Nonpolar - Polar System				
J C <sub>3</sub> H <sub>8</sub> - C <sub>2</sub> H <sub>5</sub> OH	97	325.00 - 500.00	0.323 - 62.742	[20]
K n-C <sub>5</sub> H <sub>12</sub> - CH <sub>3</sub> OH	34	372.70 - 422.60	3.471 - 25.276	[21]
L n-C <sub>5</sub> H <sub>12</sub> - C <sub>2</sub> H <sub>6</sub> CO	33	372.70 - 422.60	3.661 - 16.358	[22]
M C <sub>6</sub> H <sub>6</sub> - CH <sub>3</sub> OH	93	298.15 - 337.85	0.233 - 4.178	[23]
N n-C <sub>6</sub> H <sub>14</sub> - CH <sub>3</sub> OH	30	333.15 - 333.15	0.760 - 1.497	[24]
4. Multicomponents System				
O C <sub>3</sub> H <sub>6</sub> CO - CH <sub>3</sub> OH - H <sub>2</sub> O	110	373.15 - 523.15	1.234 - 81.634	[25]
P n-C <sub>5</sub> H <sub>12</sub> - CH <sub>3</sub> OH - C <sub>3</sub> H <sub>6</sub> CO	36	372.70 - 372.70	5.378 - 8.236	[26]

\* n.d. is the number of data points.

Table 2. Correlated results for four mixing rules

Sys.	G <sup>E</sup> model	Mixing Rule							
		WS		MBV2		TWO		CWSM	
		DP/P (%)	DY x100	DP/P (%)	DY x100	DP/P (%)	DY x100	DP/P (%)	DY x100
1. Nonpolar - Nonpolar System									
A	UNIQAC	2.81	4.70	2.54	0.89	1.44	0.74 <sup>a</sup>	1.55	0.53
	NRTL	2.33	0.63	2.74	0.87			1.68	0.53
	Wilson	3.05	0.74	2.36	0.89			1.49	0.54

Continued Table 2.

B	UNIQUAC	1.29	1.86	1.01	1.89	1.12	1.95	1.11	1.98
C	UNIQUAC	0.60	0.28	0.70	0.38	0.62	0.32	0.69	0.36
D	UNIQUAC	1.89	1.34	1.96	1.37	2.05	2.24	2.20	1.65
E	UNIQUAC	0.47	0.66	0.41	0.96	0.46	0.95	0.42	1.23

## 2. Polar - Polar System

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F	UNIQUAC	1.02	1.01	1.63	1.12	0.99	1.08 <sup>b</sup>	1.52	1.21
	NRTL	1.08	1.21	1.05	1.03			1.07	1.15
	Wilson	1.41	1.23	1.75	1.10			1.76	1.11
G	UNIQUAC	0.94	0.39	1.40	0.67	1.01	0.56	1.22	0.60
H	UNIQUAC	1.80	1.20	1.75	1.12	2.42	1.26	1.77	1.24
I	UNIQUAC	1.78	1.21	2.33	0.99	3.23	1.29	1.97	1.02

## 3. Nonpolar - Polar System

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J	UNIQUAC	4.42	3.24	7.45	2.06	2.75	1.79 <sup>c</sup>	4.72	1.96
	NRTL	4.37	2.28	7.17	2.00			4.49	1.88
	Wilson	5.39	2.01	7.37	1.99			4.65	1.90
K	UNIQUAC	1.04	1.18	1.77	1.05	4.66	2.24	1.39	1.75
L	UNIQUAC	0.40	0.60	1.08	0.75	1.33	1.05	0.39	0.61
M	UNIQUAC	0.84	0.84	1.71	1.04	4.96	2.63	1.25	1.11
N	UNIQUAC	0.60	0.75	5.31	3.49	6.97	4.18	3.46	2.07
Grand Average		1.73	1.34	2.33	1.32	2.43	1.59	2.05	1.44

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a For nonpolar-nonpolar systems two parameters  $k_{12}$ ,  $k_{21}$  are needed.

b For polar-polar systems three parameters  $k_{12}$ ,  $k_{21}$ ,  $\beta_{12}$  ( $\beta_{12} = \beta_{21}$ ) are needed.

c For polar-nonpolar systems four parameters  $k_{12}$ ,  $k_{21}$ ,  $\beta_{12}$ ,  $\beta_{21}$  are needed.

Table 3. Predicated results for four mixing rules

Sys. $G^E$ model	Mixing Rule								
	WS		MHV2		TWM		CWSM		
	DP/P (%)	DY $\times 100$	DP/P (%)	DY $\times 100$	DP/P (%)	DY $\times 100$	DP/P (%)	DY $\times 100$	
1. Polar - Polar System									
F UNIQUAC[27] <sup>a</sup>	2.10	1.41	1.74	1.18	1.03	1.11	[16] <sup>b</sup>	1.57	1.30
NRTL [27]	2.67	1.55	3.69	1.74				2.43	1.25
Wilson [27]	3.37	1.69	4.94	2.18				3.22	1.41
G UNIQUAC[28]	2.33	1.53	2.00	0.86	1.59	0.75	[17]	1.39	0.70
NRTL [28]	4.74	2.30	6.55	2.41				2.52	1.13
Wilson [28]	2.41	1.46	4.70	2.20				4.72	1.89
I UNIQUAC[29]	3.48	1.07	3.46	1.43	3.73	1.40	[18]	5.96	1.51
NRTL [29]	4.07	1.31	3.35	1.63				5.62	1.21
Wilson [29]	4.91	1.03	2.12	0.88				6.50	1.18
2. Nonpolar - Polar System									
L UNIQUAC[30]	3.23	1.85	5.70	2.42	1.23	0.57	[22] <sup>c</sup>	2.76	0.79
M UNIQUAC[31]	12.22	5.03	18.60	7.68	6.00	3.09	[23]	5.12	3.28
N UNIQUAC[32]	25.39	9.74	37.73	11.19	6.58	4.18	[24]	7.58	3.43
3. Multicomponent System									
O UNIQUAC	1.61	1.98	3.50	1.63	2.84	2.09		1.53	1.71
P UNIQUAC	9.32	2.45	22.95	4.82	3.17	1.11		12.20	2.94
Grand Average	5.85	2.46	8.65	3.02	3.27	1.79		4.51	1.70

a, b The numbers in the parentheses indicate the reference number, where the parameters of  $G^E$  model, and the VLE data at low pressure are gotten, respectively.

c  $\beta_{12}$  and  $\beta_{21}$  are needed.